

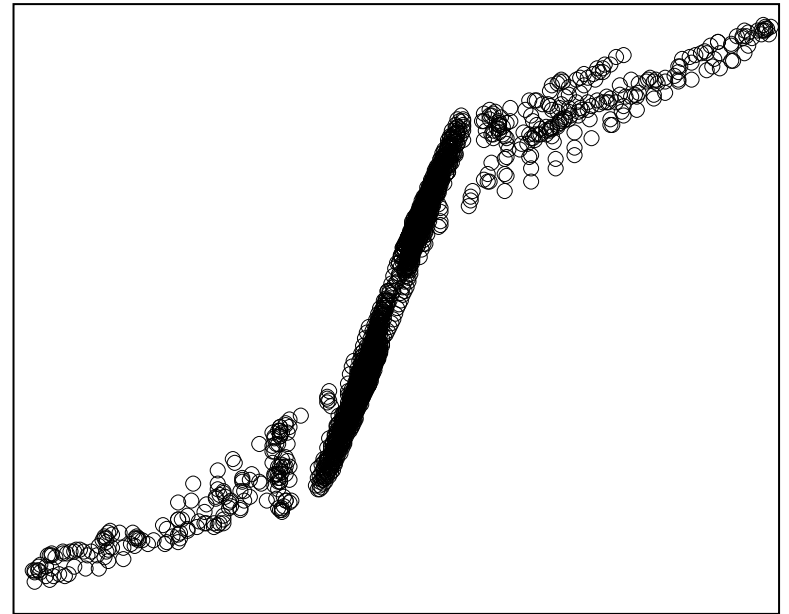
Détection, caractérisation et identification de non-linéarités en dynamique des structures

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Mots-Clefs

- Acoustique
- Vibrations
- Expérimentations
- Basses Fréquences (autour de 200Hz et inférieures)

Applications

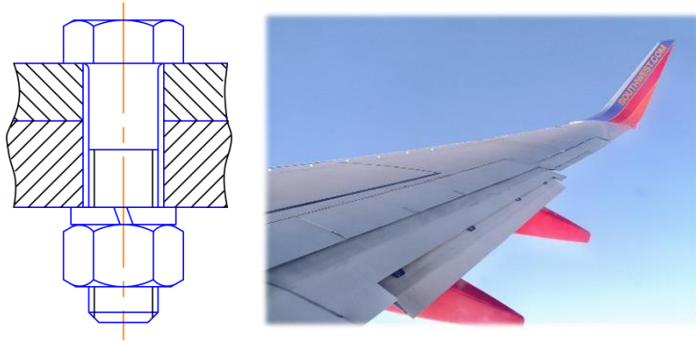
- Transports
- Bâtiments
- Environnement
- Surveillance
- Contrôle et synthèse
- Musique
- Audio...

Thèmes

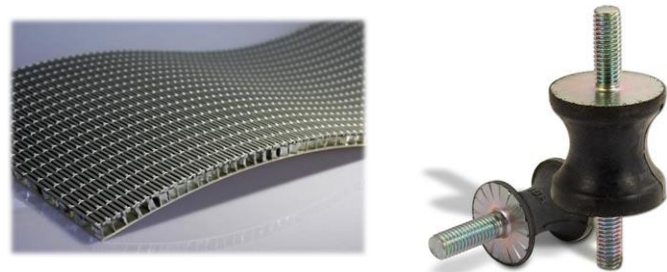
- Conception d'Expériences
- Outils et Méthodes en Basses Fréquences
- Perception
- Systèmes dynamiques non linéaires
- Traitement du Signal
- Capteurs
- Propagation...

Is Your Application Nonlinear ?

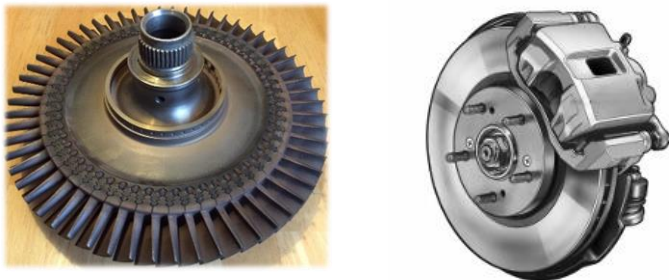
Bolts, joints and gaps



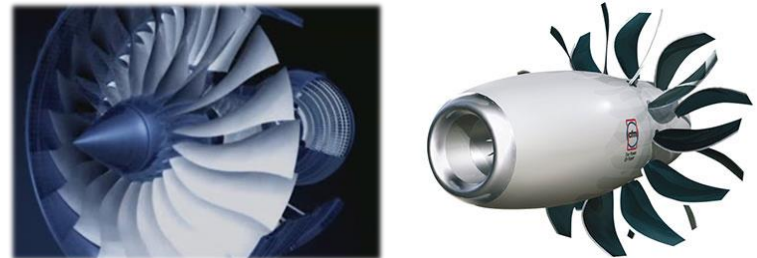
Elastomers and composites



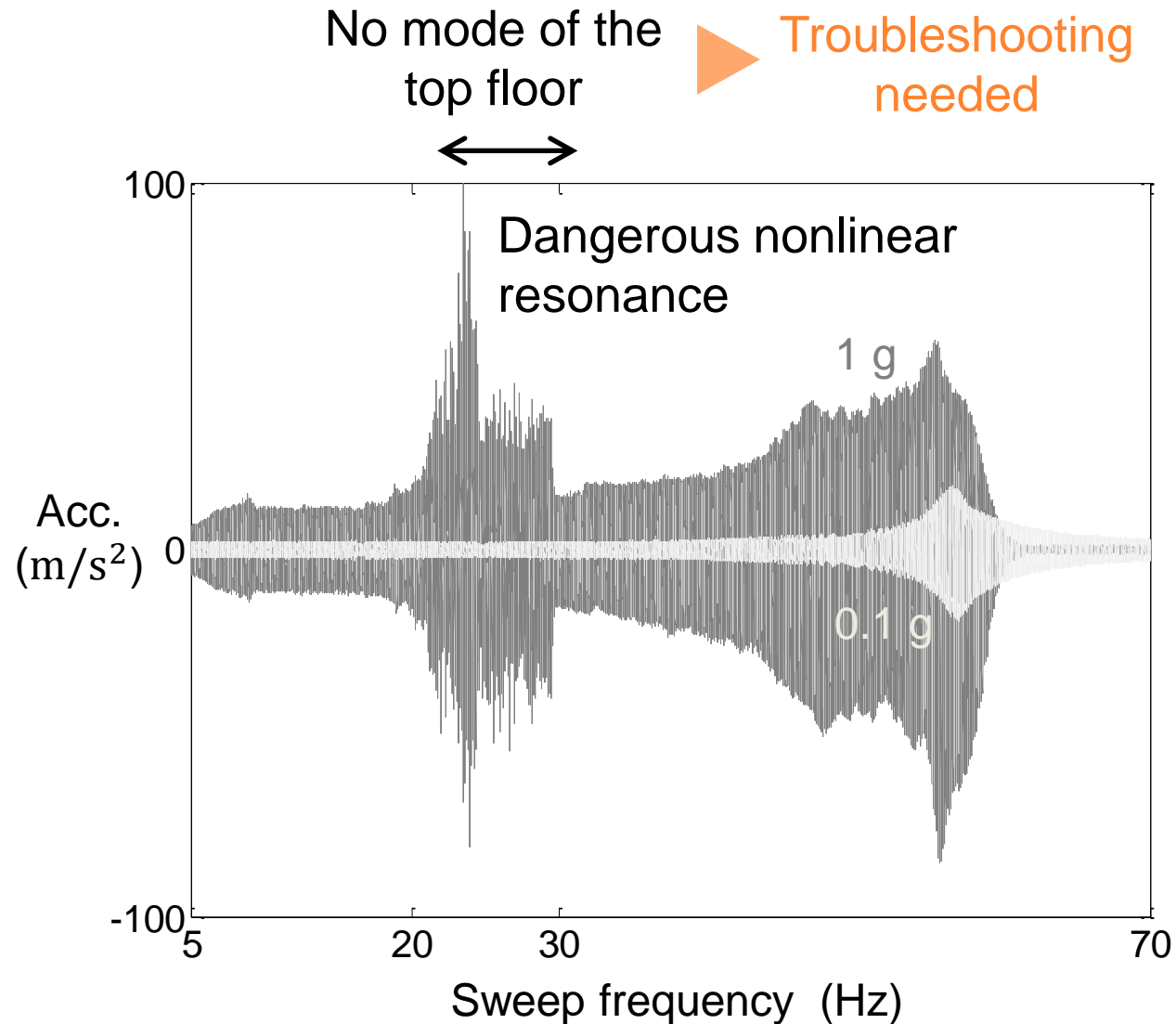
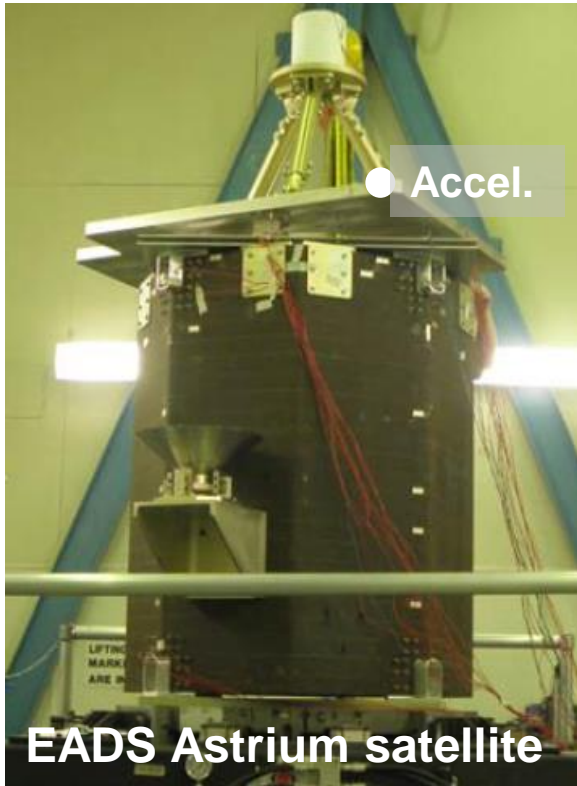
Friction and contact



Large amplitudes

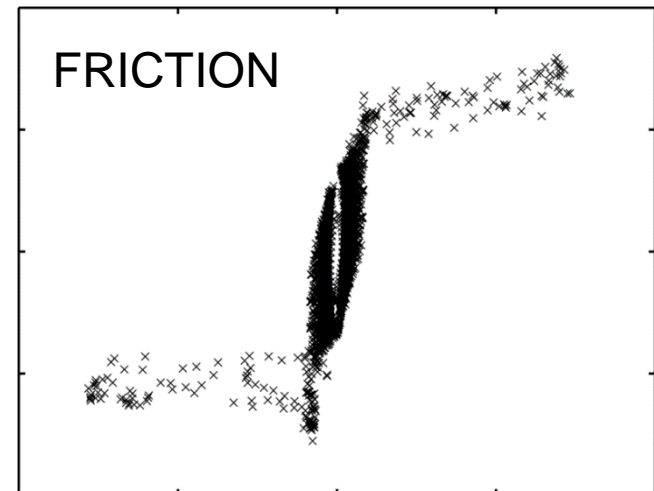
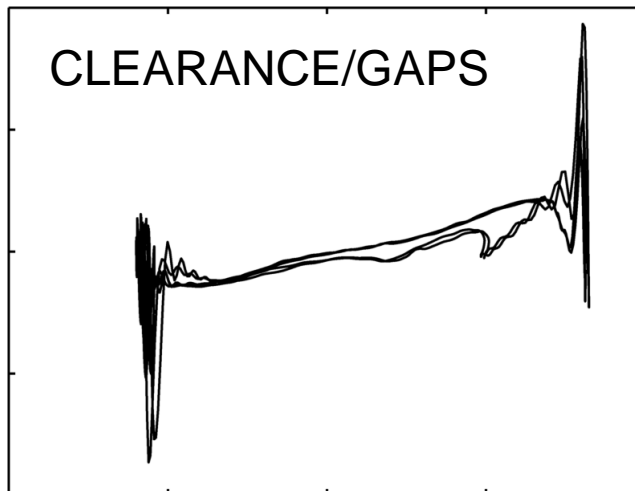
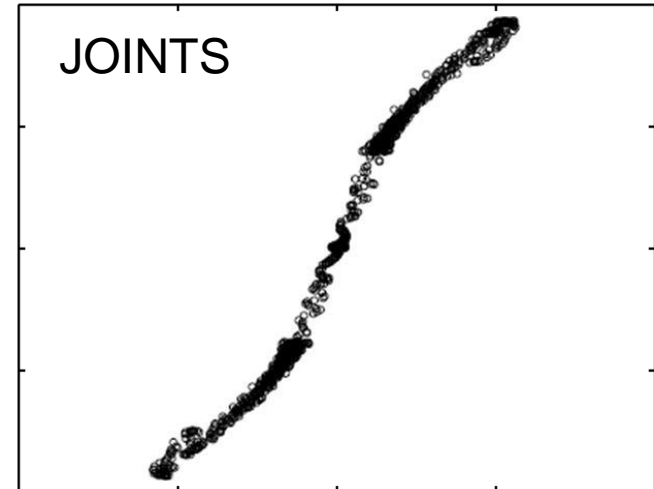
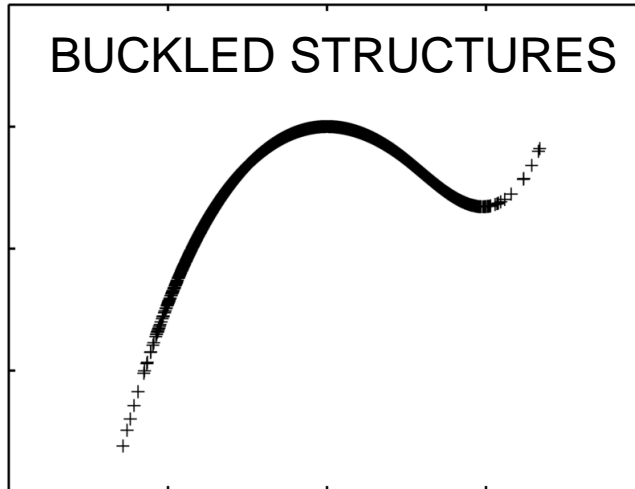


Why Should You Care About Nonlinearity ?



Why Is Nonlinear System Identification Difficult ?

Individualistic nature of structural nonlinearities.

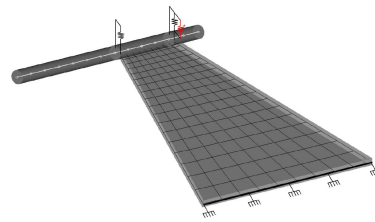


The Big Picture

VIBRATION
MEASUREMENTS



LINEAR FINITE
ELEMENT MODEL



MEASURE

IDENTIFY

HYBRID
MODELING

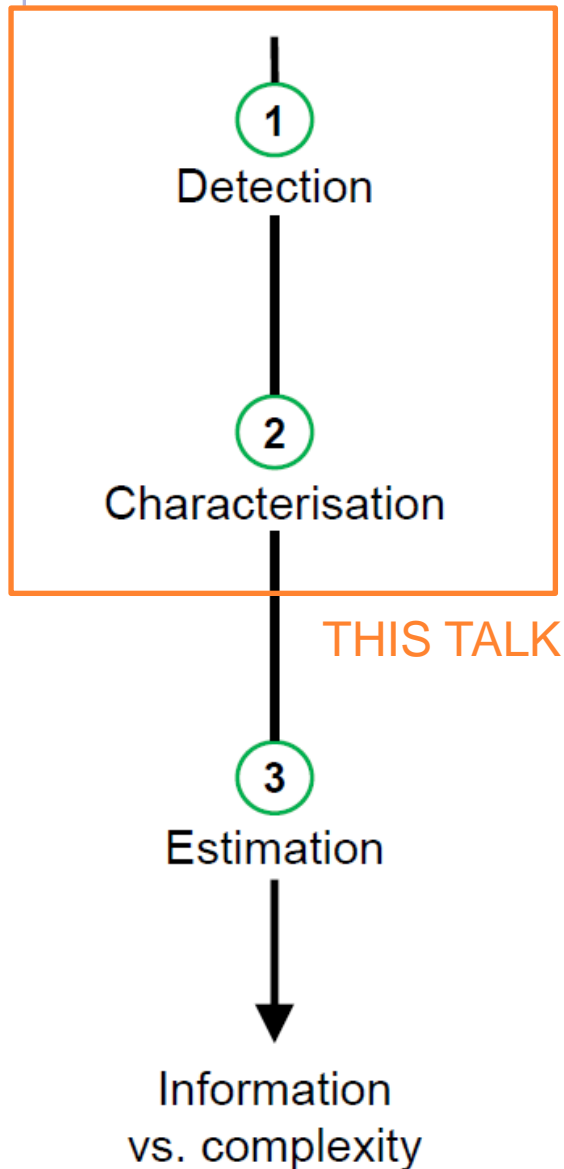
UNDERSTAND

DESIGN

*Identify nonlinear
connections early on*

*Compute nonlinear
features and responses*

The Nonlinear System Identification Process



Do I observe nonlinear effects?
Should I build a nonlinear model?

Where is the nonlinearity located ?
What is the underlying physics?
What mathematical model?

Model parameters?
How uncertain are they?

NSI of a Full-Scale Aerospace Structure



Decommissioned F-16 aircraft, Belgian Airforce Base.
Collaboration with Siemens LMS.

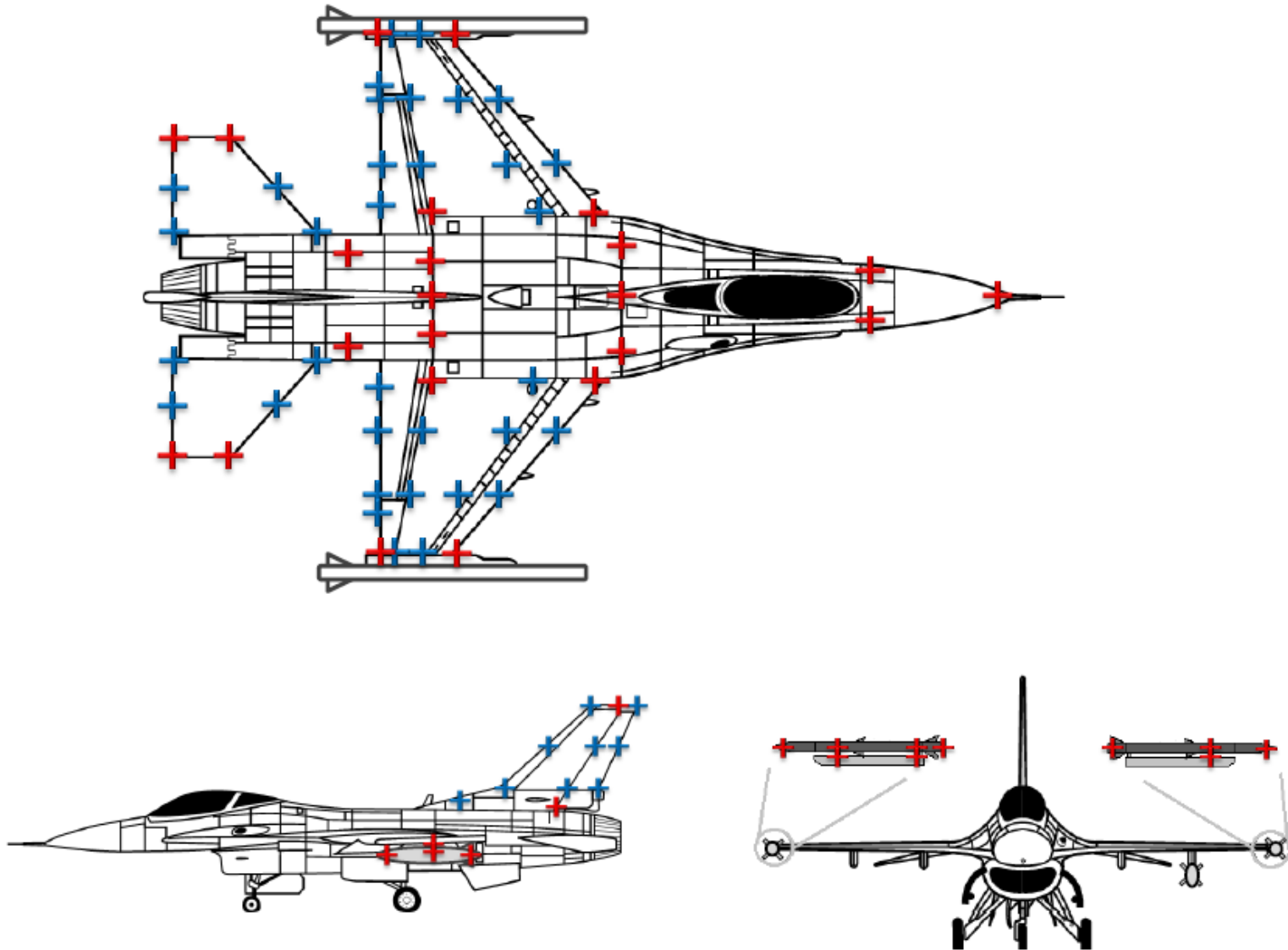
Testing Campaign, September 2014



Resting on the landing gears with flat tires; control surfaces held fixed.

Two shakers underneath the wings (sine sweep, random, multisine force signals).

Sensor Set-Up (>160 Accelerometers)



A Specific Testing Campaign

3 different excitation signals: random, sine sweep, multisine

Consider multiple levels of excitations/types of excitations.

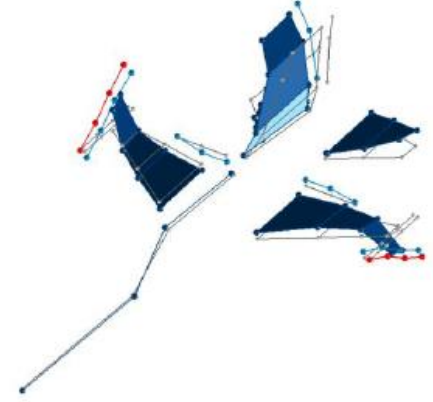
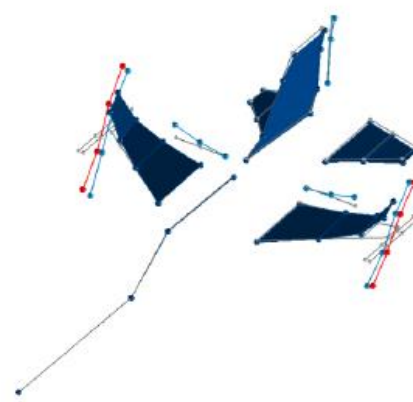
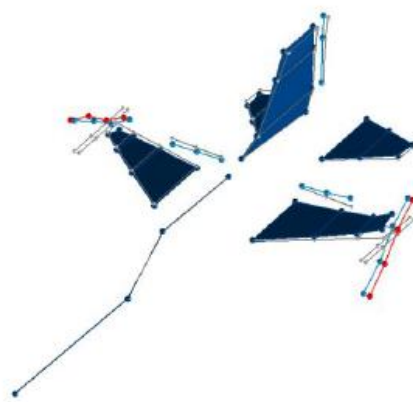
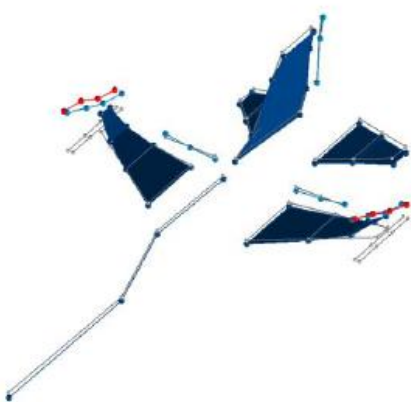
Record throughput time histories.

Measure the force signal.

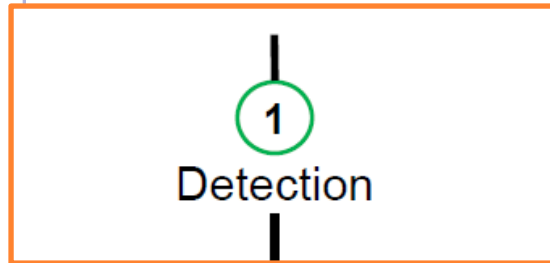
Instrument potential nonlinearities with sensors on both sides.

Linear Modal Analysis at Low Level

Modes	Natural Frequency	Damping Ratio
RBM (roll motion)	3.5 Hz	1.68 %
RBM (vertical motion)	3.9 Hz	2.31 %
Sym Wing bending	5.2 Hz	0.84 %
ASym Missile rotation	6.6 Hz	0.77 %
Sym Wing torsion	7.3 Hz	0.43 %
ASym Wing bending	9.1 Hz	0.74 %



The Nonlinear System Identification Process



1
Detection



Do I observe nonlinear effects?
Should I build a nonlinear model?

Where is the nonlinearity located ?
What is the underlying physics?
What mathematical model?

Model parameters?
How uncertain are they?

2

Characterisation

3

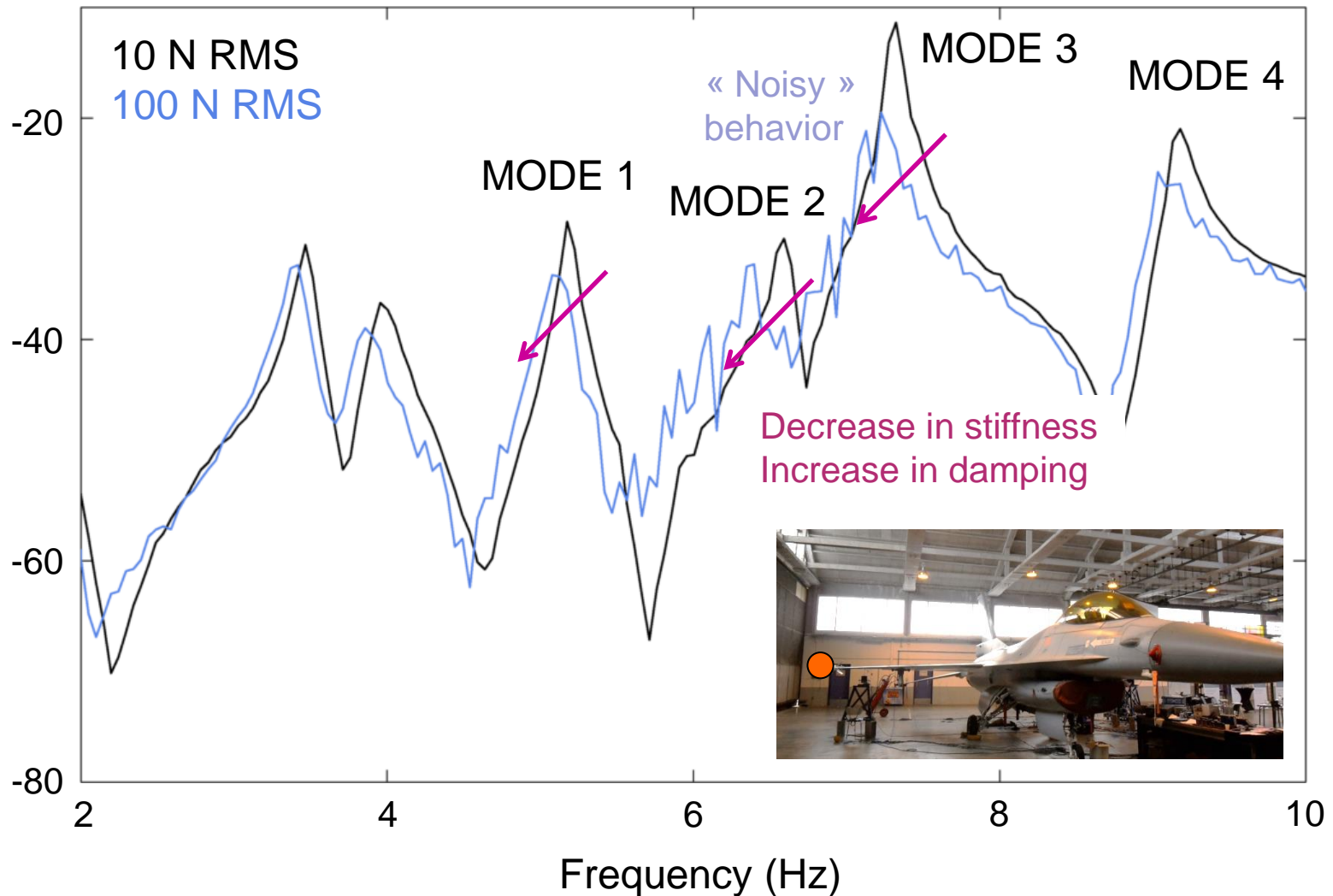
Estimation



Information
vs. complexity

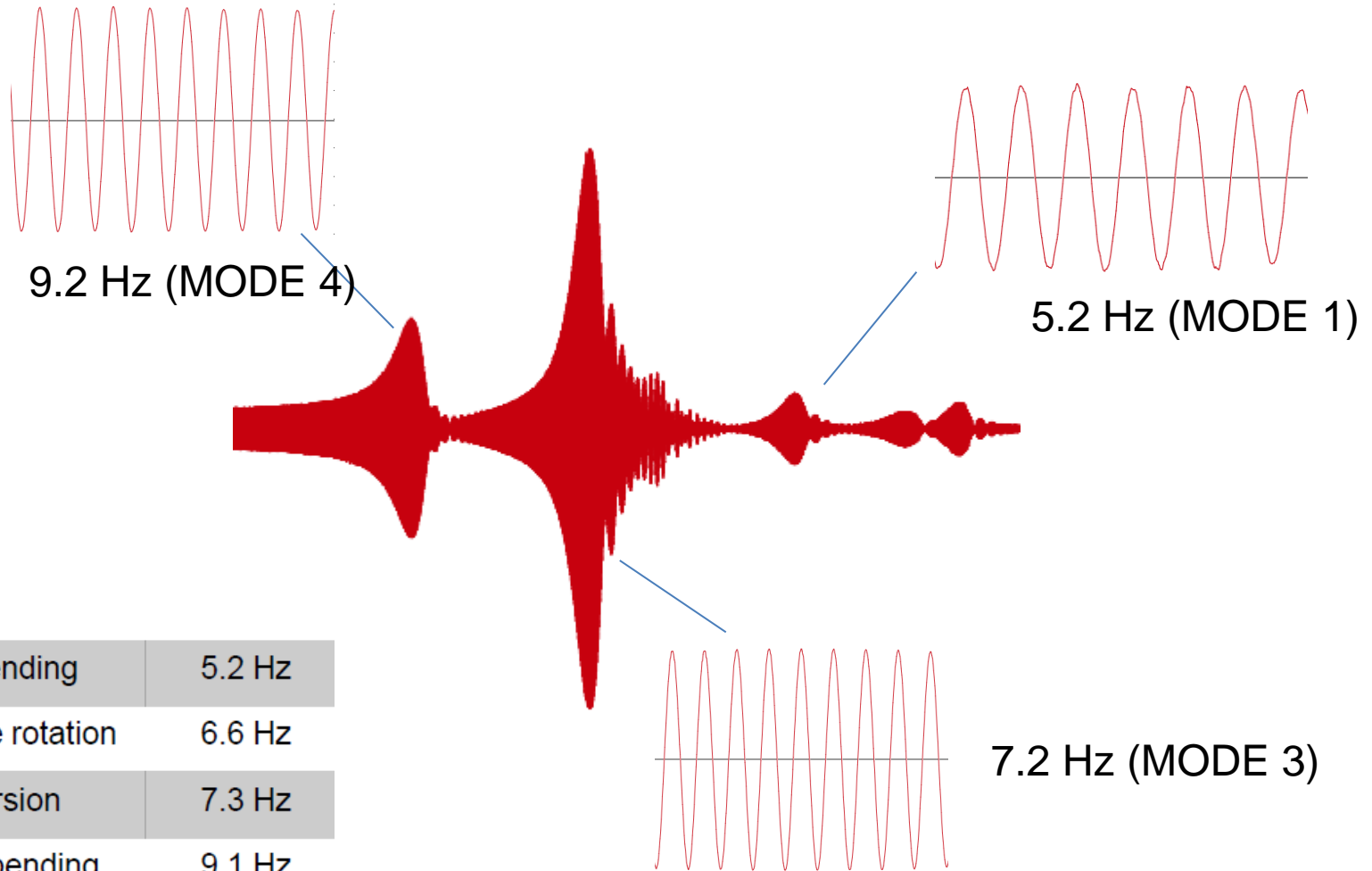
Homogeneity Test (FRFs at Several Levels)

Excitation: random



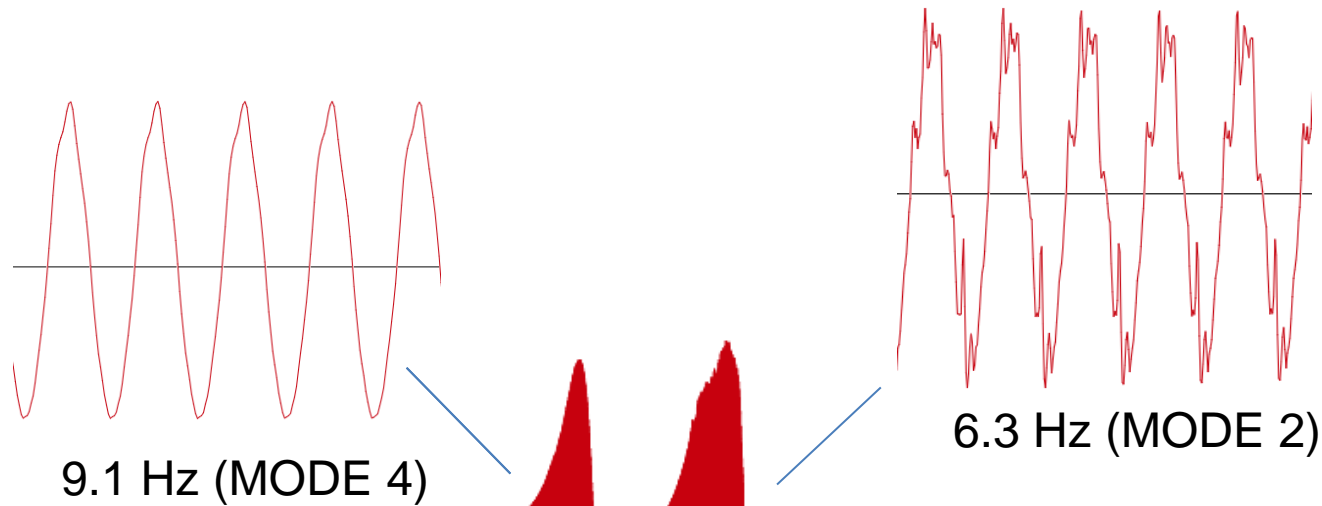
Time Series at Low Level (Right Missile)

Excitation: sine sweep down

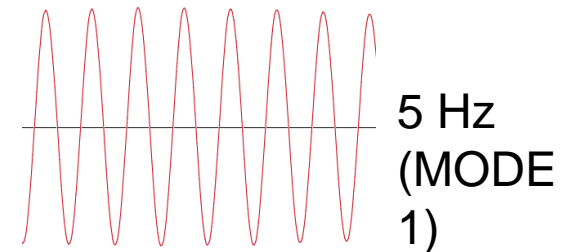
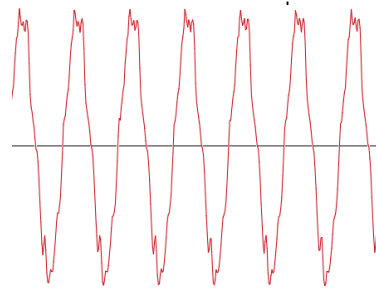
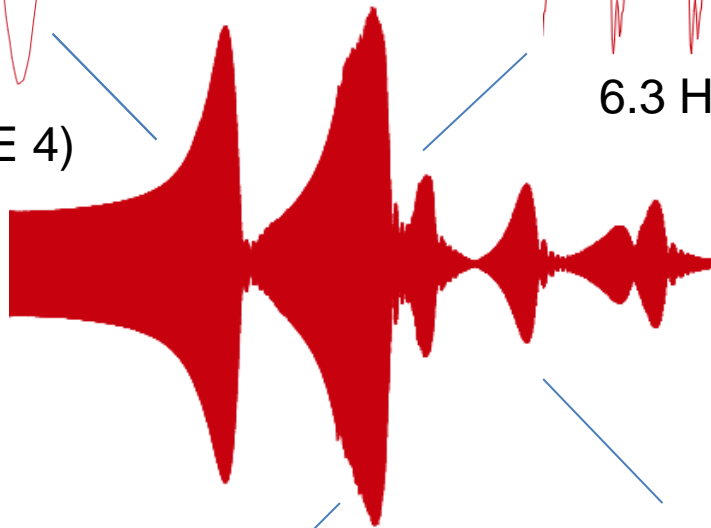


Sym Wing bending	5.2 Hz
ASym Missile rotation	6.6 Hz
Sym Wing torsion	7.3 Hz
ASym Wing bending	9.1 Hz

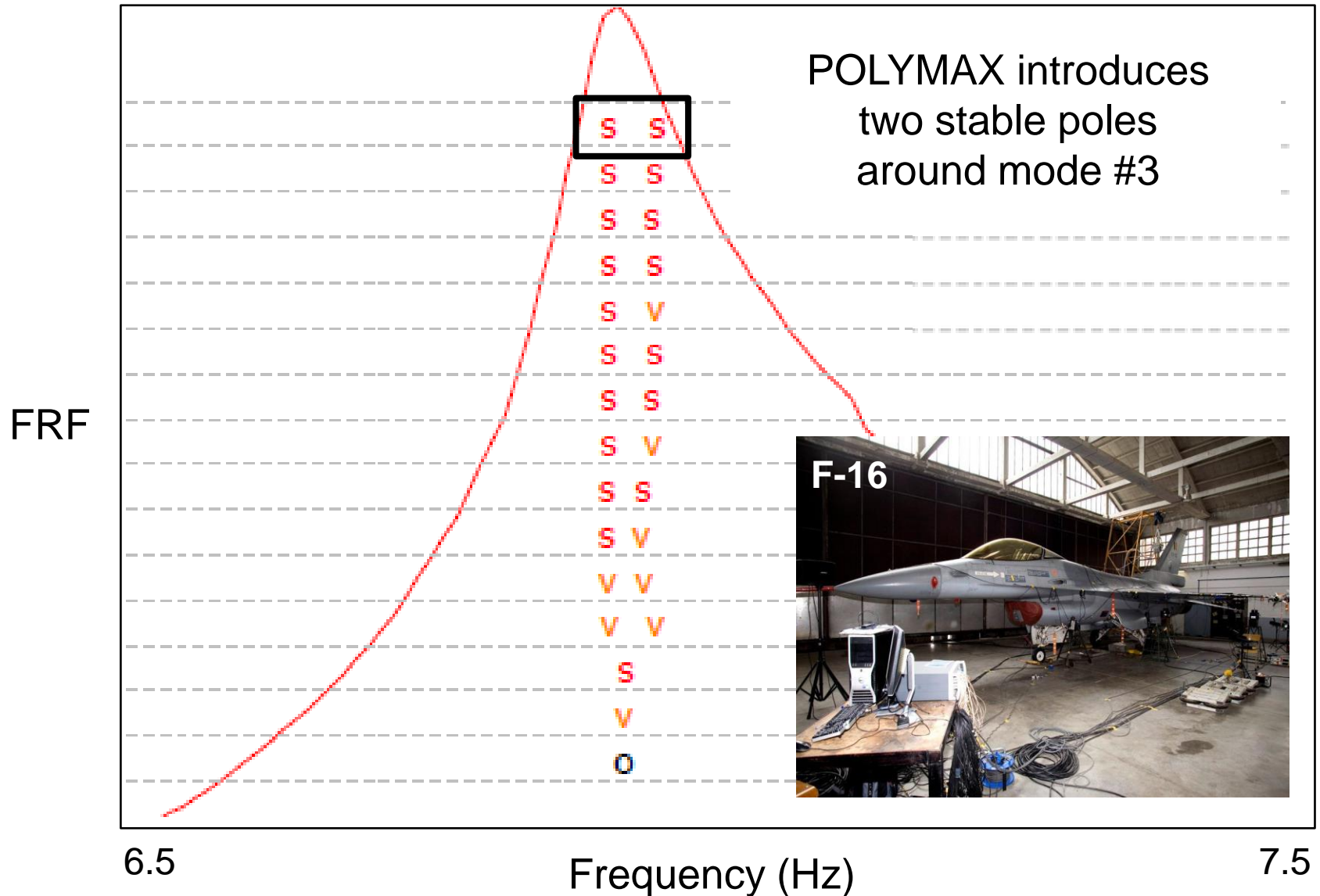
Time Series at High Level (Right Missile)



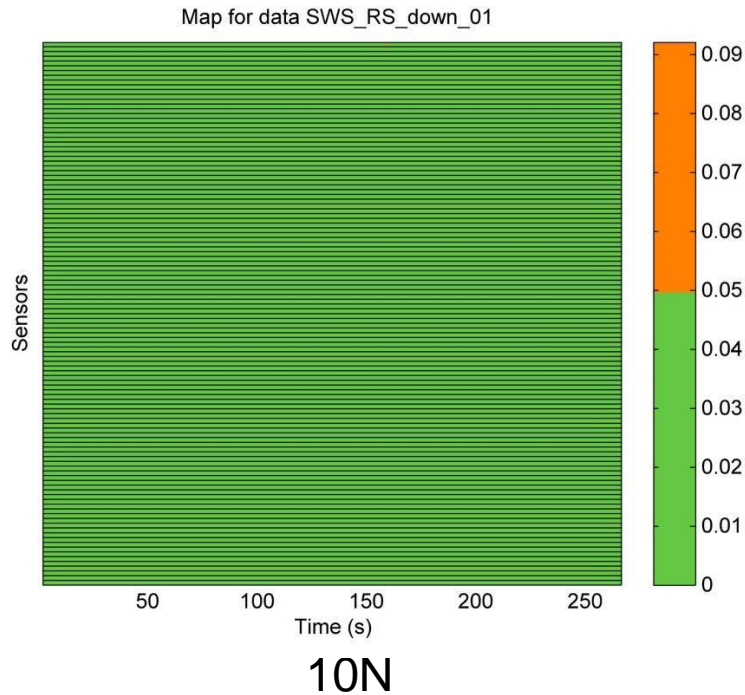
Sym Wing bending	5.2 Hz
ASym Missile rotation	6.6 Hz
Sym Wing torsion	7.3 Hz
ASym Wing bending	9.1 Hz



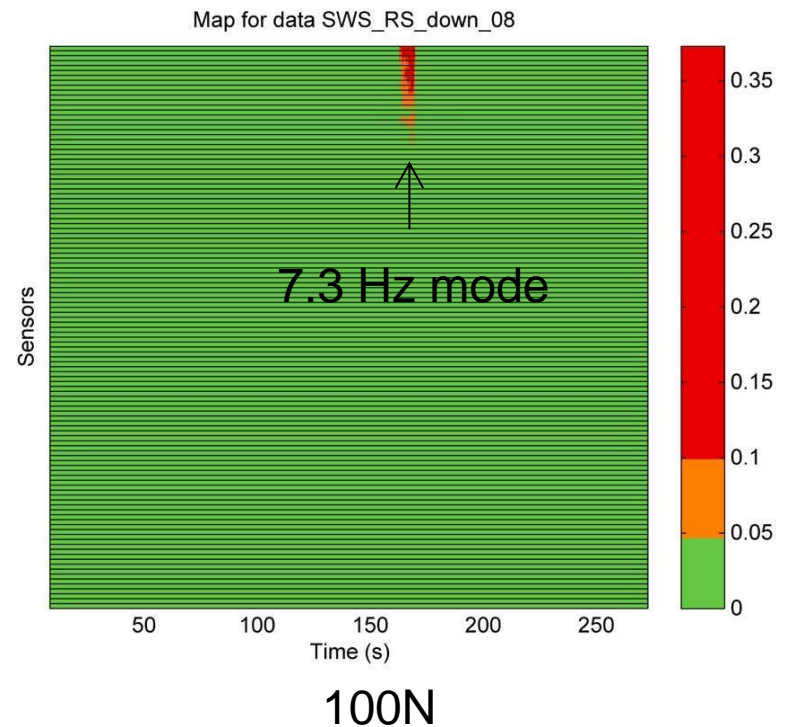
Failure of Linear Modal Analysis at High Level



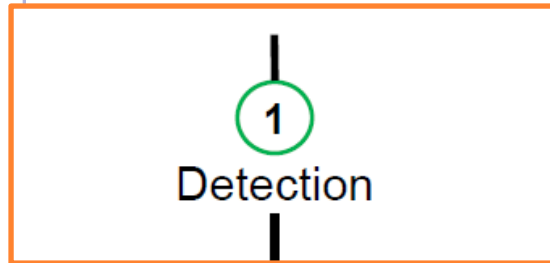
Map for Nonlinearity Detection



Highlight a departure from planar motion in phase space



The Nonlinear System Identification Process



1
Detection



Do I observe nonlinear effects? **YES**
Should I build a nonlinear model?

Where is the nonlinearity located ?
What is the underlying physics?
What mathematical model?

Model parameters?
How uncertain are they?

2
Characterisation

3
Estimation

Information
vs. complexity

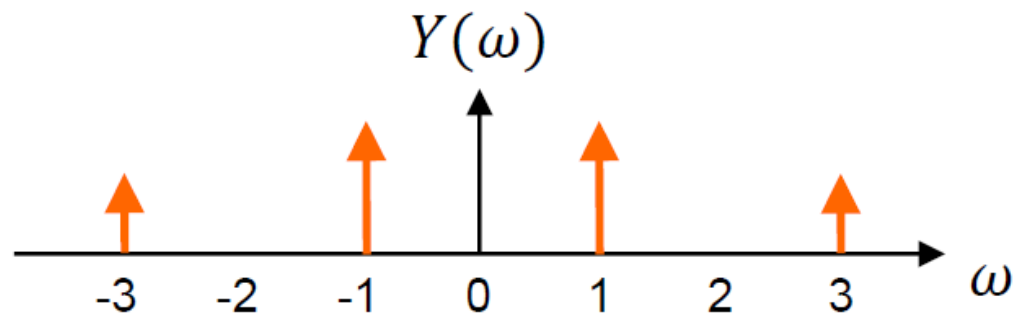
Nonlinearity Distortions

Output of a cubic nonlinearity:

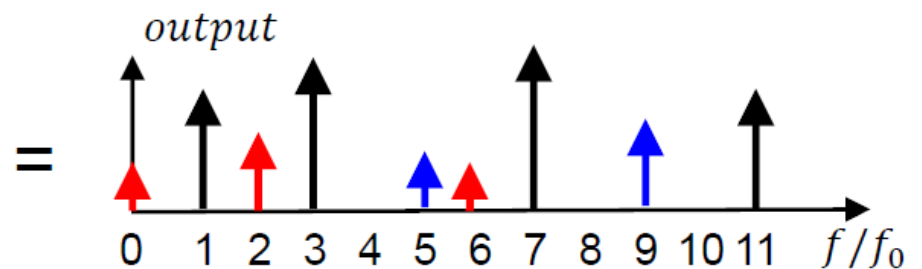
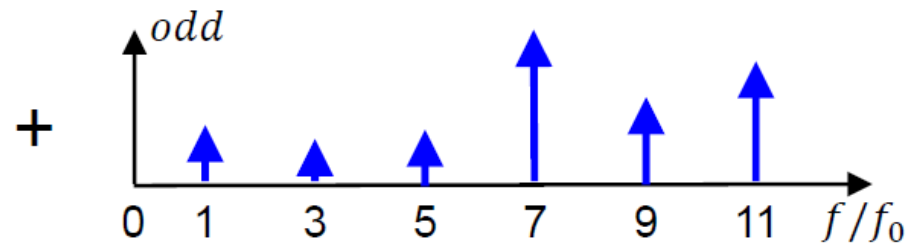
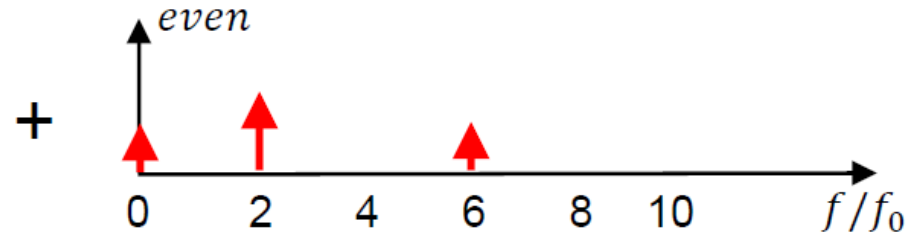
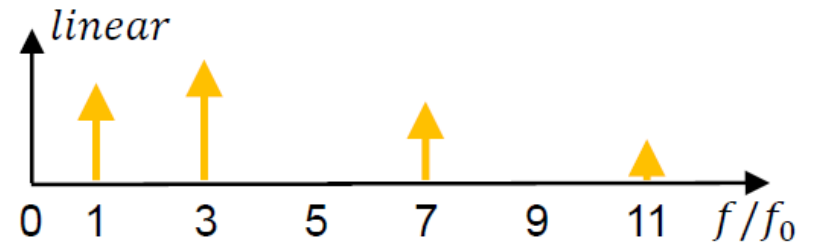
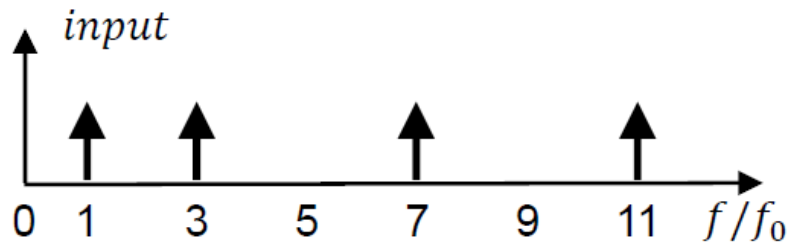
$$\begin{aligned} y(t) &= u^3(t) \\ &= (e^{j\omega t} - e^{-j\omega t})(e^{j\omega t} - e^{-j\omega t})(e^{j\omega t} - e^{-j\omega t}) \end{aligned}$$

All possible combinations, 3 by 3, of the frequencies -1 and 1.

1	1	1	3
1	1	-1	1
1	-1	1	1
1	-1	-1	-1
-1	1	1	1
-1	1	-1	-1
-1	-1	1	-1
-1	-1	-1	-3

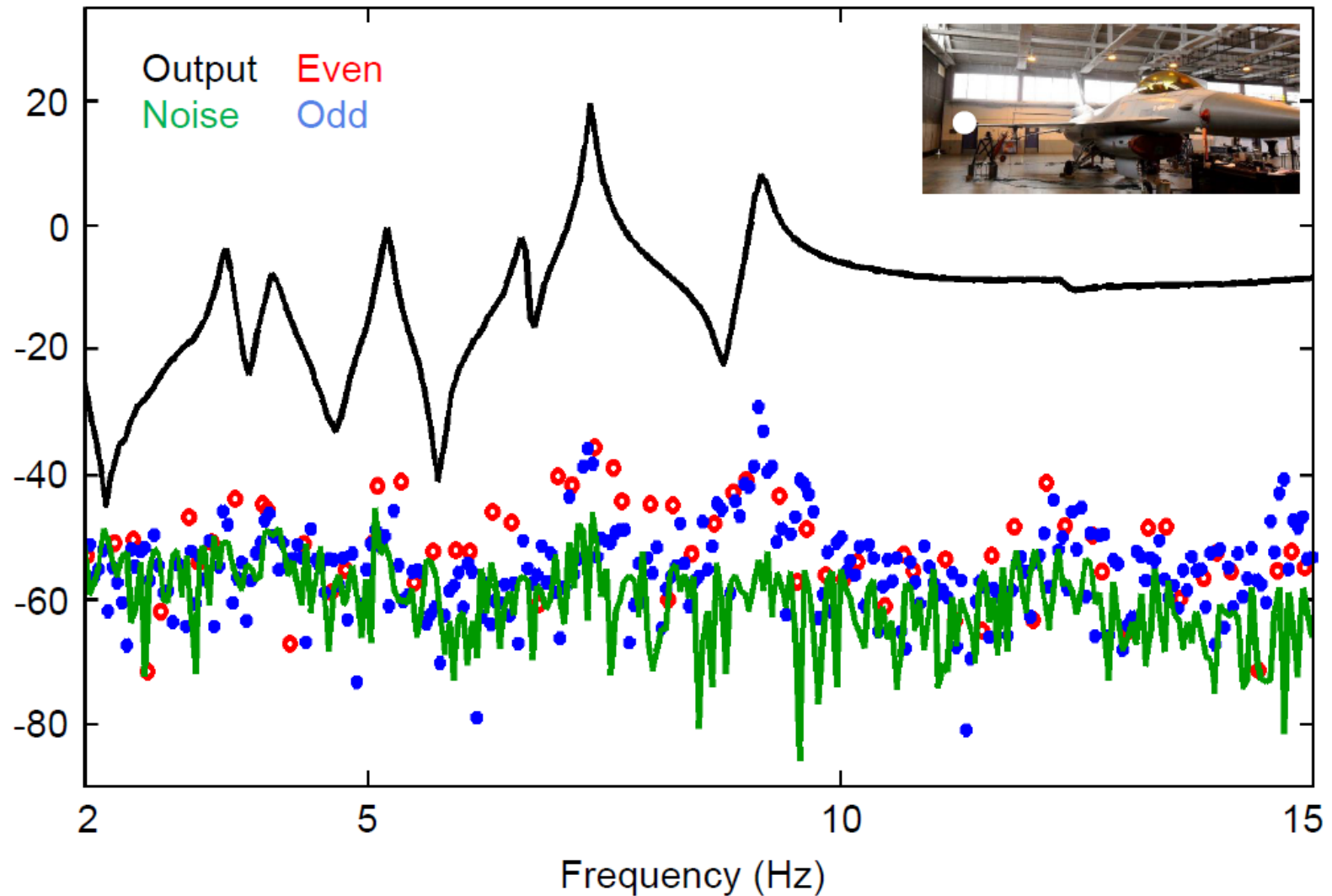


A Carefully Selected Input Spectrum



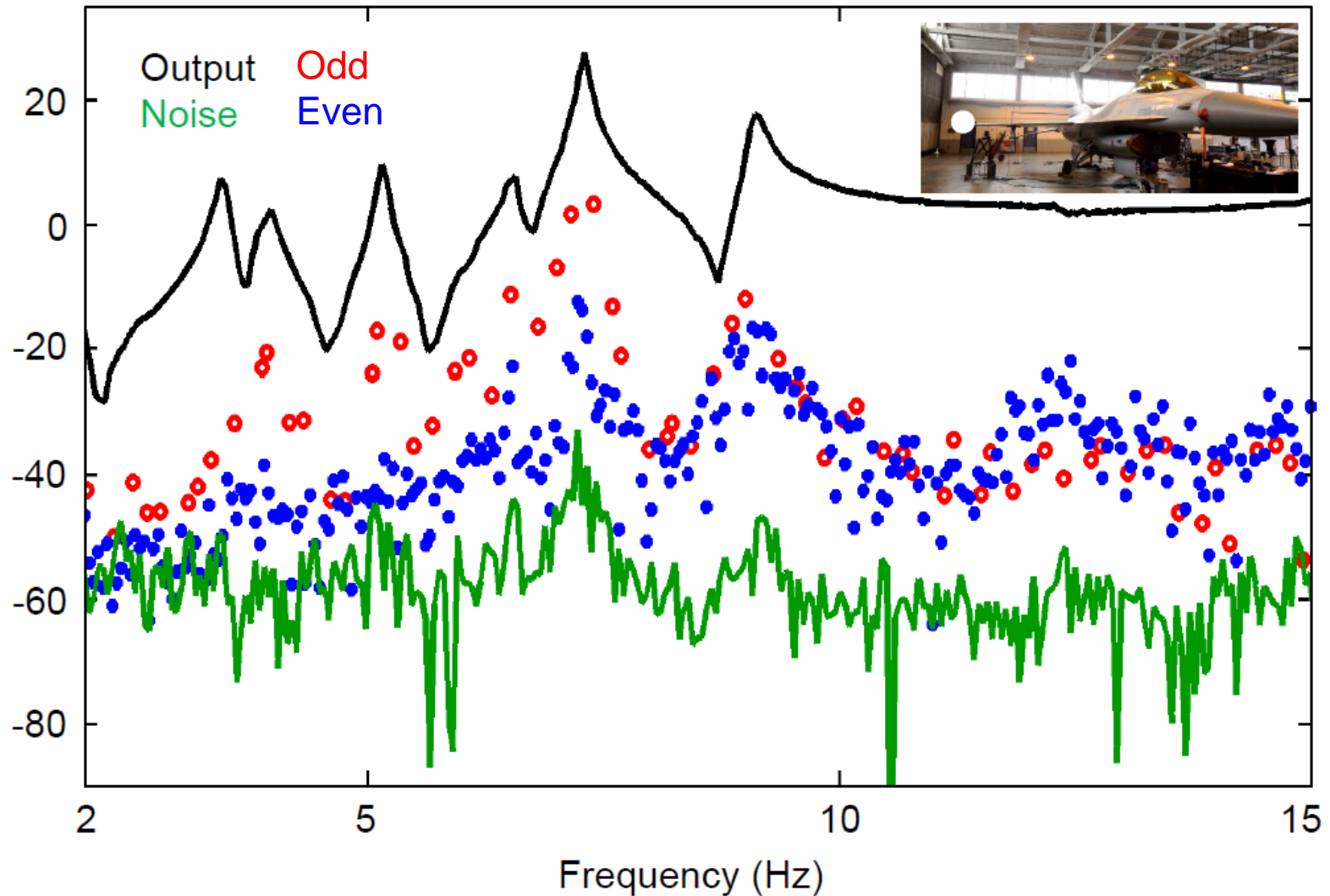
Negligible Distortions at Low Level

Amplitude (dB)

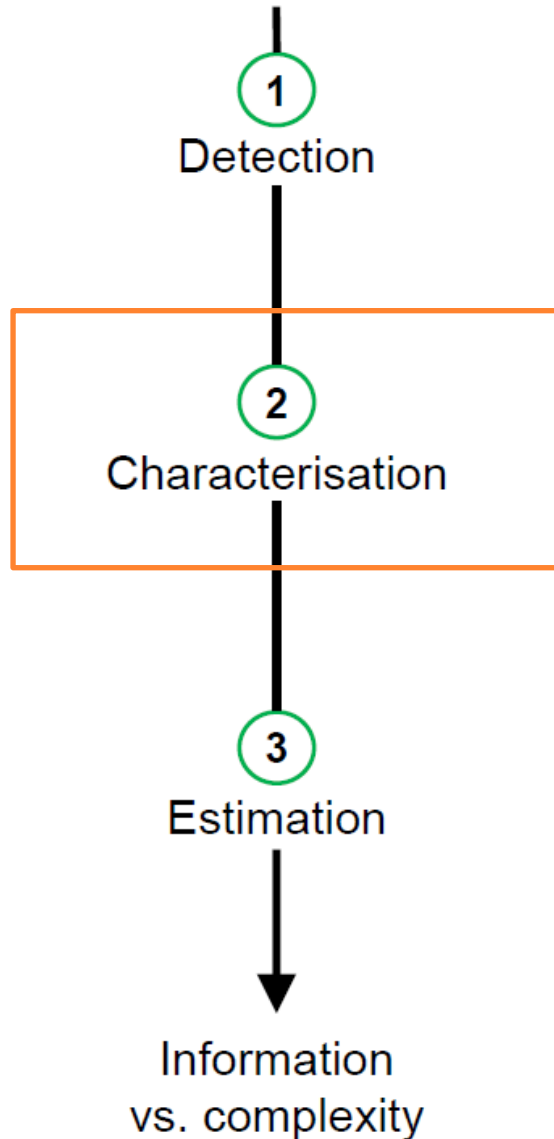


Important Distortions at High Level

Amplitude (dB)



The Nonlinear System Identification Process



Do I observe nonlinear effects? **YES**

Should I build a nonlinear model? **YES**



Where is the nonlinearity located ?

What is the underlying physics?

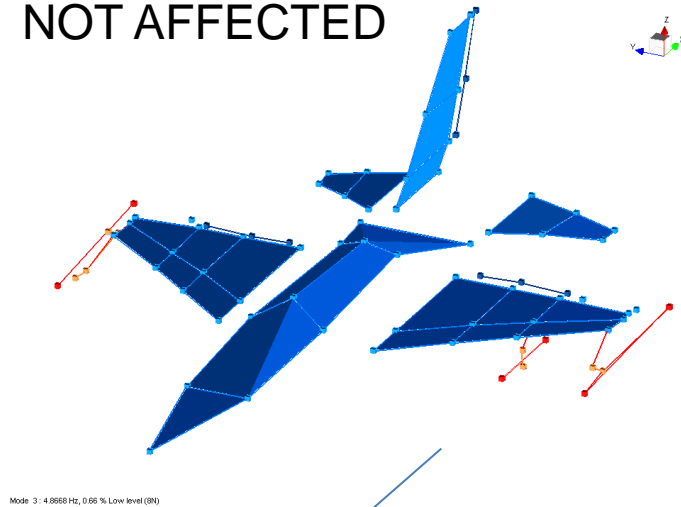
What mathematical model?

Model parameters?

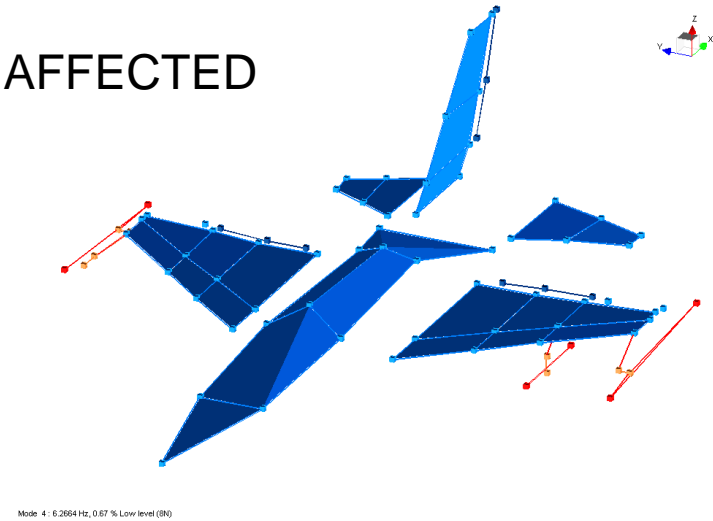
How uncertain are they?

Modal Shapes Give Useful Information

NOT AFFECTED

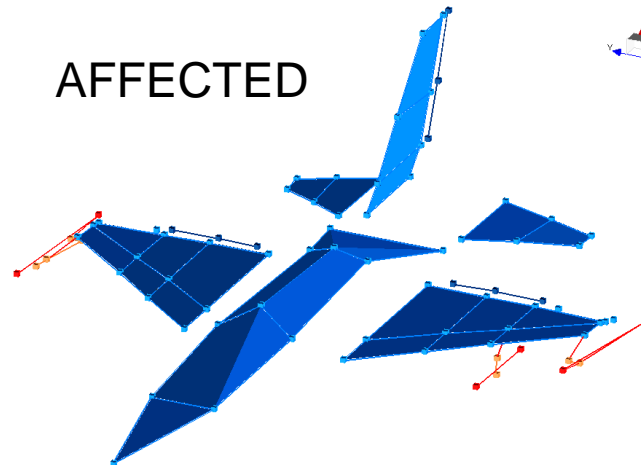


AFFECTED

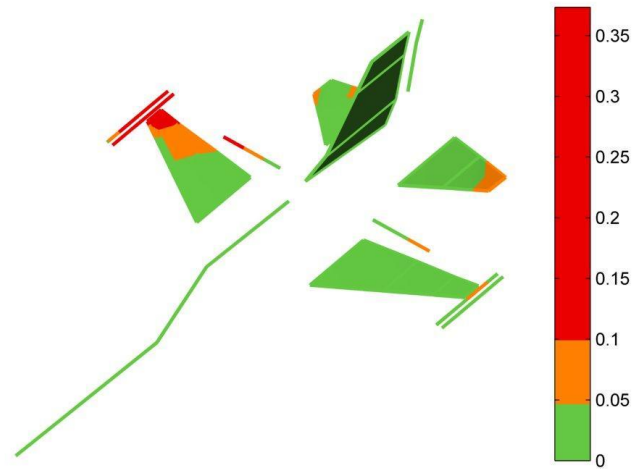
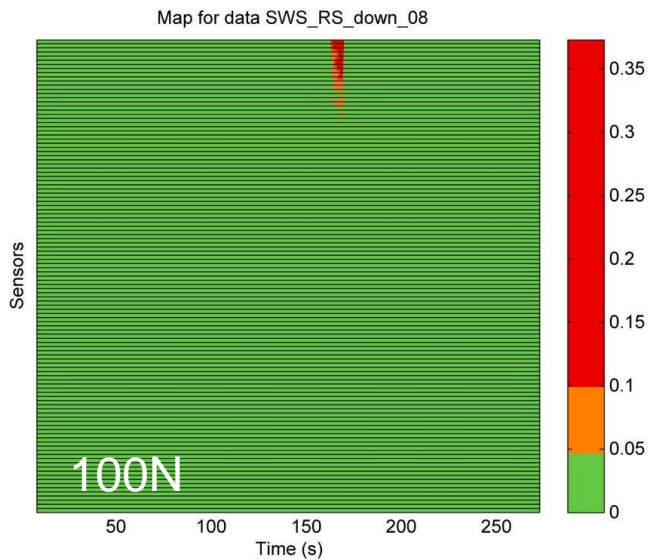
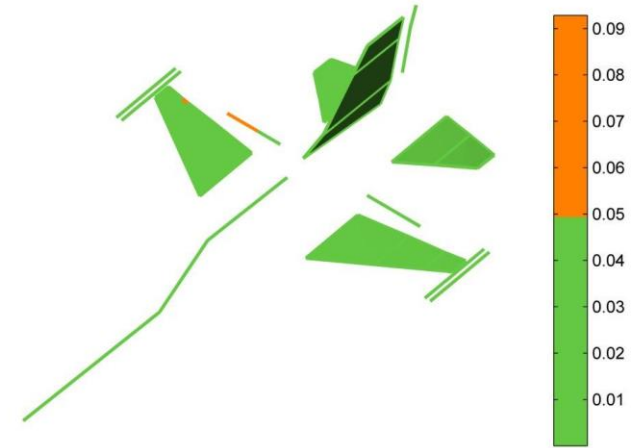
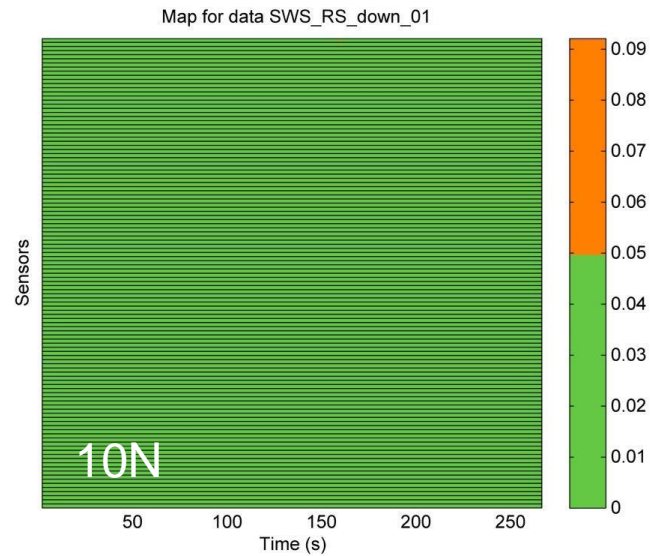


Sym Wing bending	5.2 Hz
ASym Missile rotation	6.6 Hz
Sym Wing torsion	7.3 Hz

AFFECTED



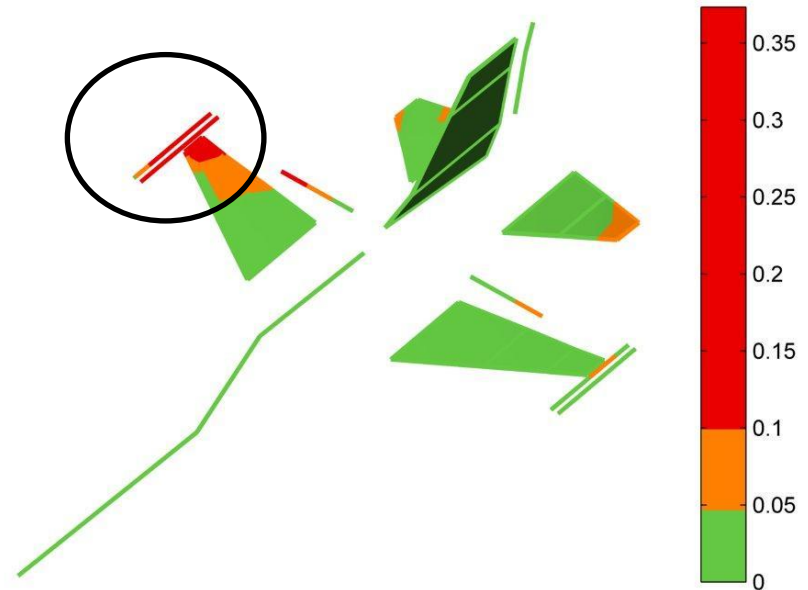
Nonlinearity at Wing Tip Is Clearly Revealed



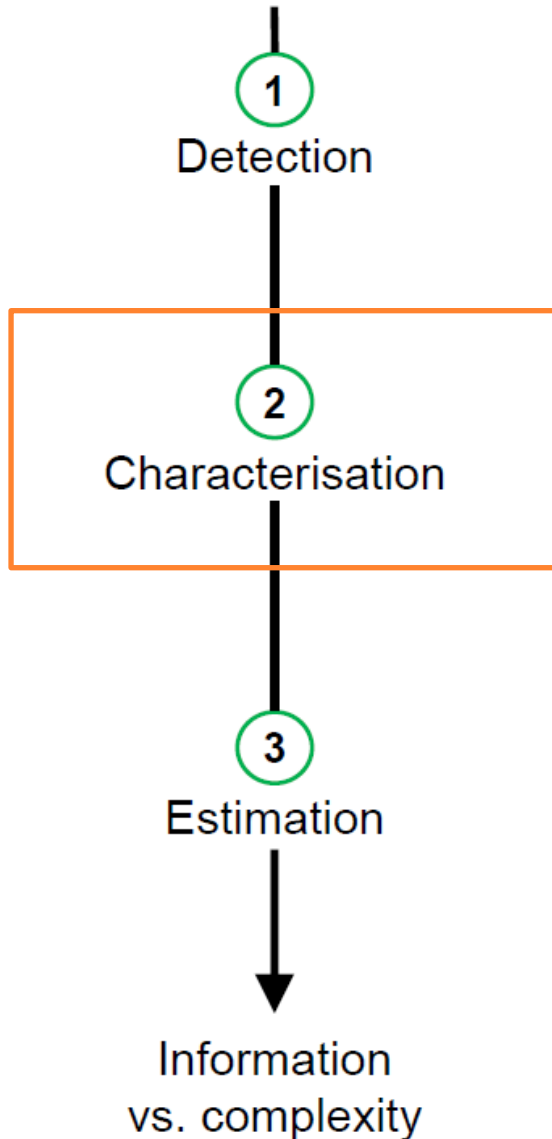
Let's Have a Closer Look at Right Wing Tip



How would you model
this connection ?



The Nonlinear System Identification Process



Do I observe nonlinear effects? **YES**

Should I build a nonlinear model? **YES**

Where is the nonlinearity located ? **WING TIP**

What is the underlying physics?

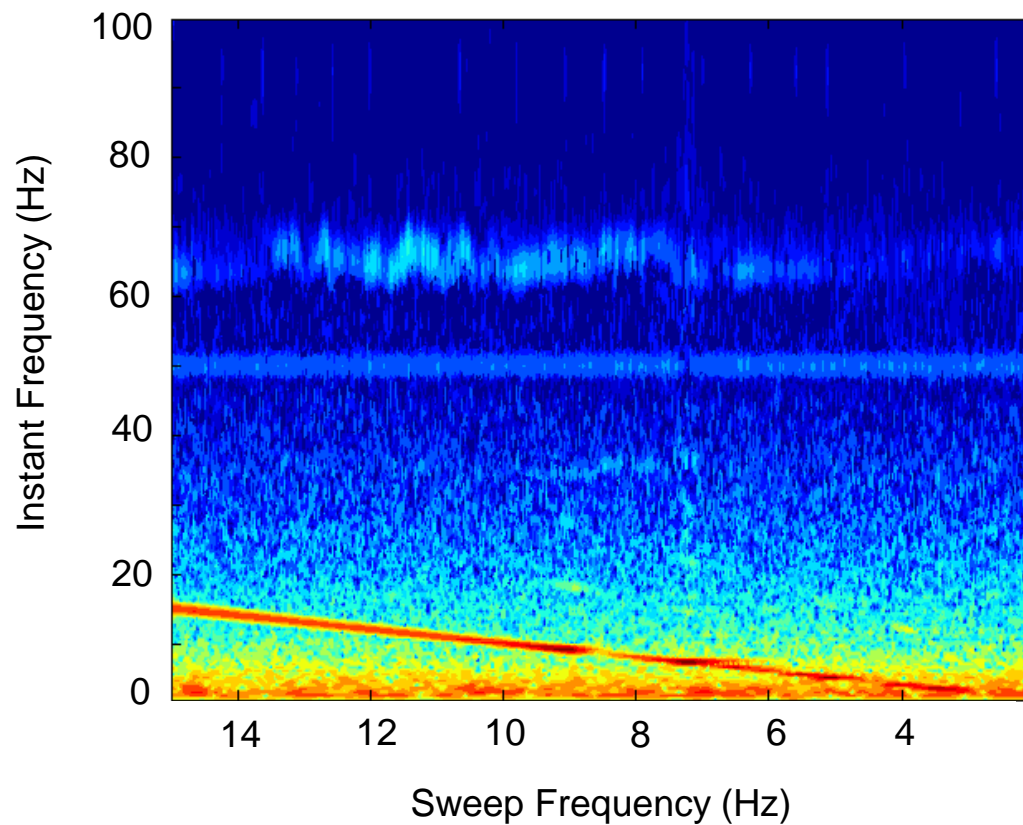
What mathematical model?

Model parameters?

How uncertain are they?

F-16: Sine Sweep Down (5N)

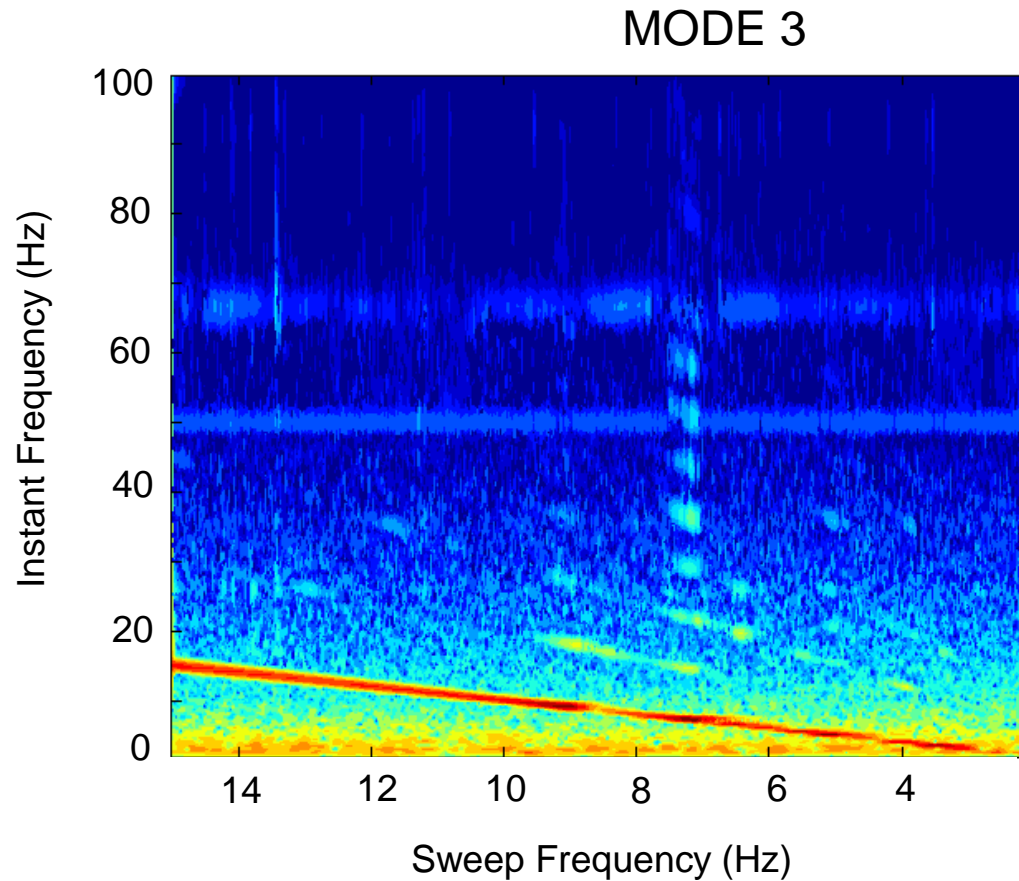
The excitation line is visible (sine sweep down)



Europe !

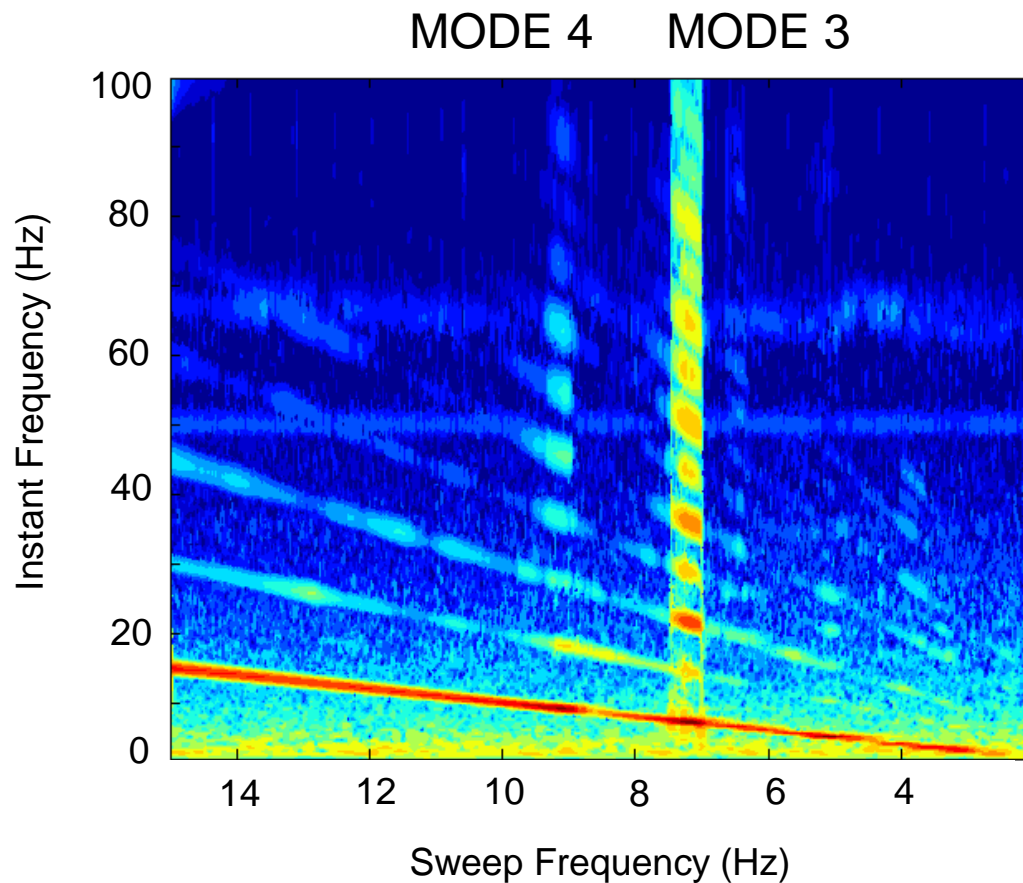
F-16: Sine Sweep Down (14N)

Harmonics and nonsmooth phenomena for mode 3



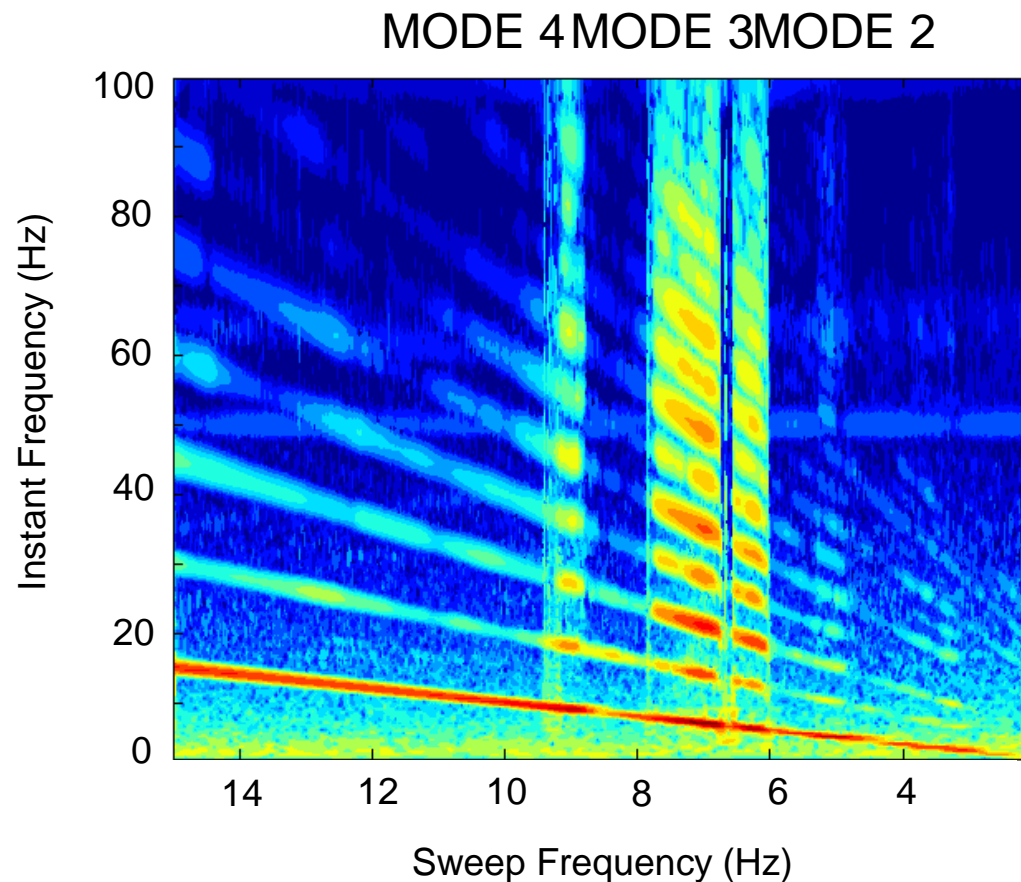
F-16: Sine Sweep Down (48N)

Some harmonics stronger than others (modal interactions ?)

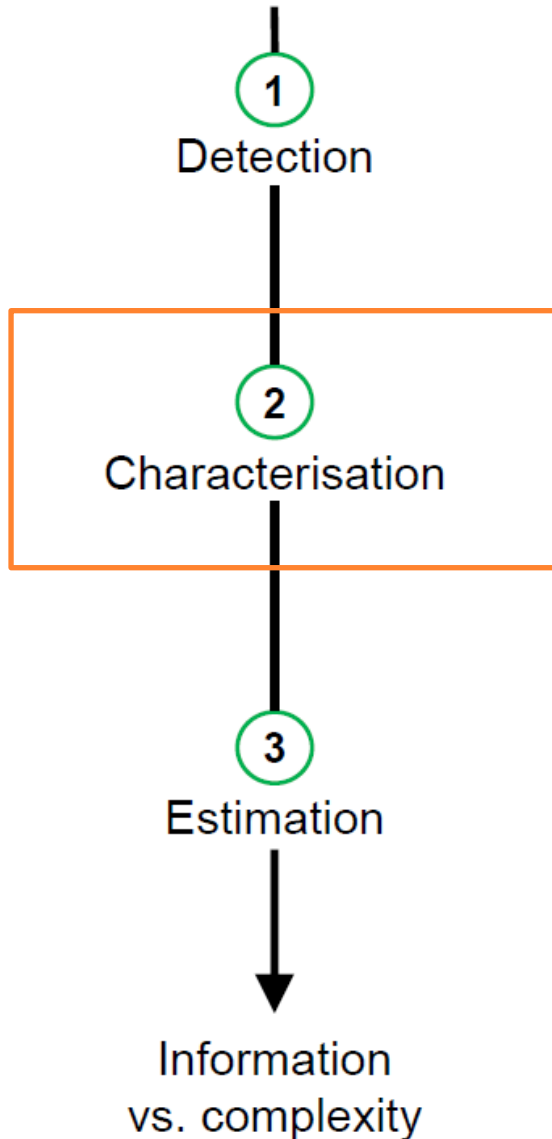


F-16: Sine Sweep Down (96N)

Several modes affected by nonlinearity



The Nonlinear System Identification Process



Do I observe nonlinear effects? **YES**

Should I build a nonlinear model? **YES**

Where is the nonlinearity located ? **WING TIP**

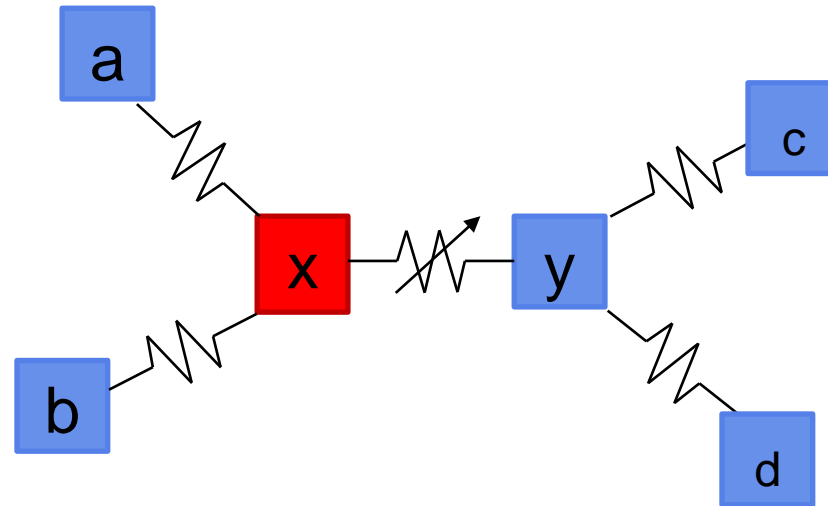
What is the underlying physics? **IMPACTS**

What mathematical model?

Model parameters?

How uncertain are they?

Can We *Visualize* the Nonlinearity ?



$$m\ddot{x} + \cancel{k_1}(x - a) + \cancel{k_2}(x - b) + f_{nl}(x - y, \dot{x} - \dot{y}) = 0$$

$$f_{nl}(x - y, \dot{x} - \dot{y}) \propto \cancel{-m\ddot{x}}$$

$$f_{nl}(x - y, \dot{x} - \dot{y}) \propto -\ddot{x}$$

Build a surface
in a 3D plot

The Four Steps of the Acceleration Surface Method

1. Instrument the nonlinear connection with 2 accelerometers.

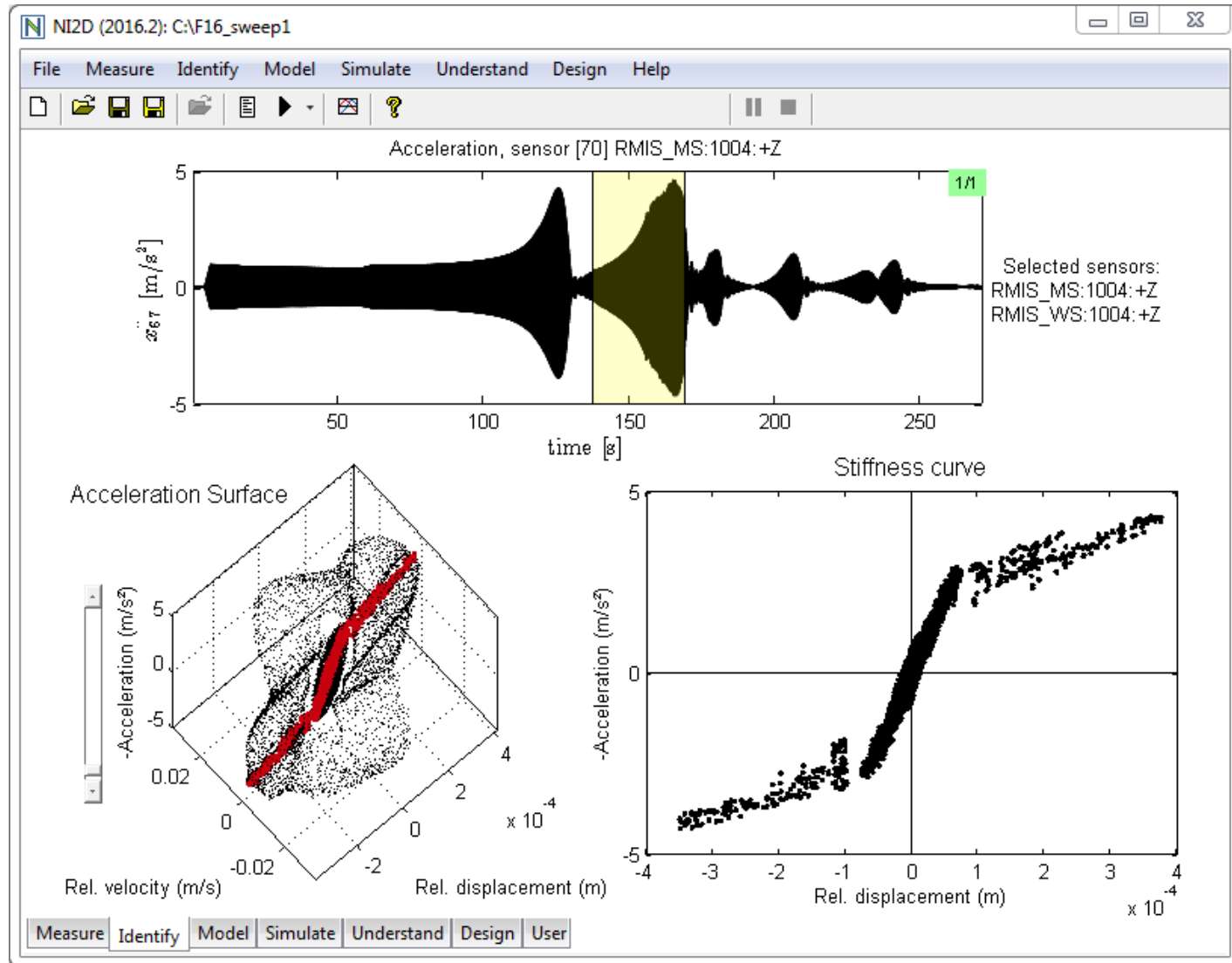


2. Integrate and filter to get displacements and velocities (Worden, MSSP, 1990).

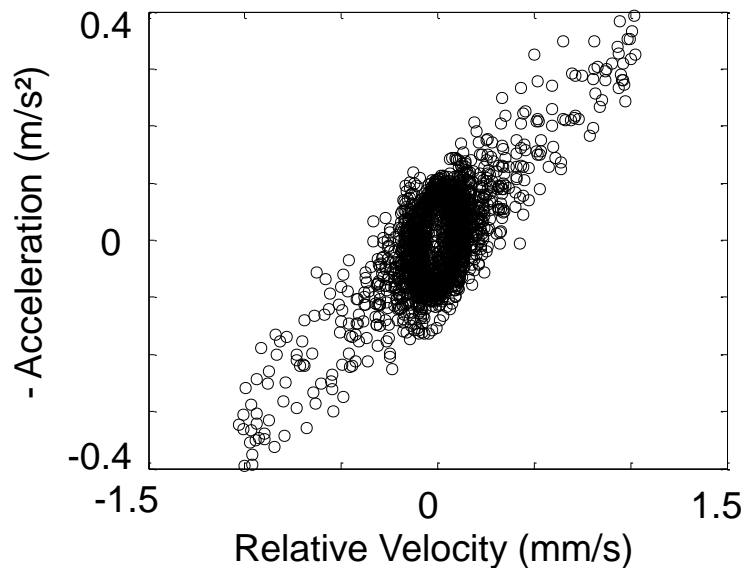
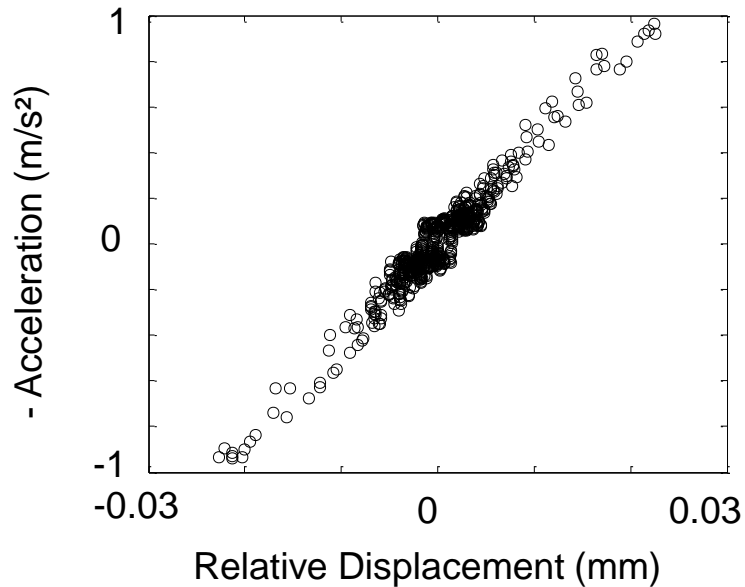
3. Calculate the 3D acceleration surface over a single mode.

4. Consider surface slices to obtain stiffness/damping curves.

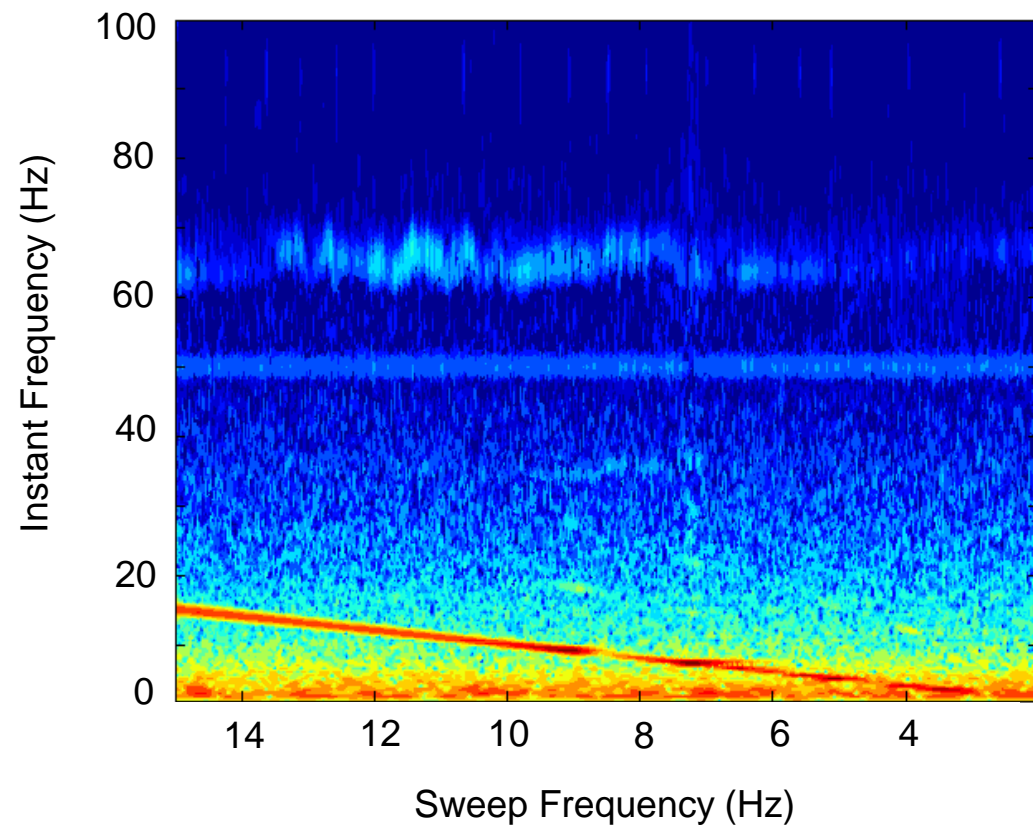
The Acceleration Surface Method



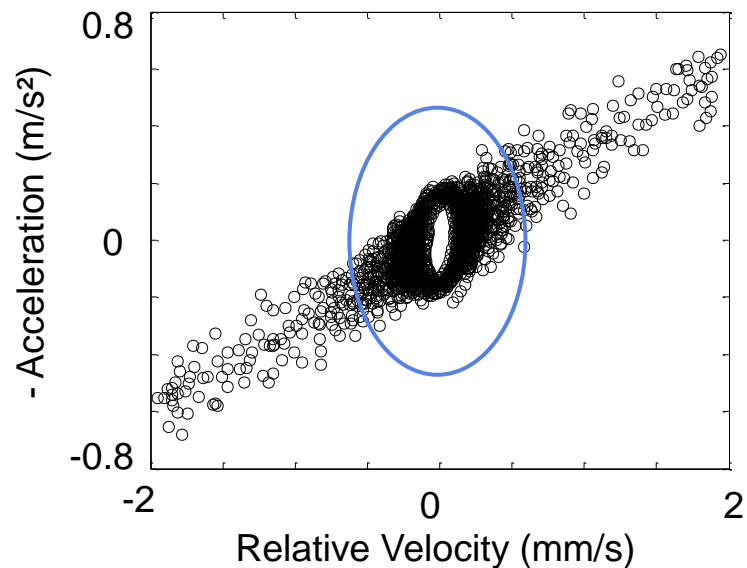
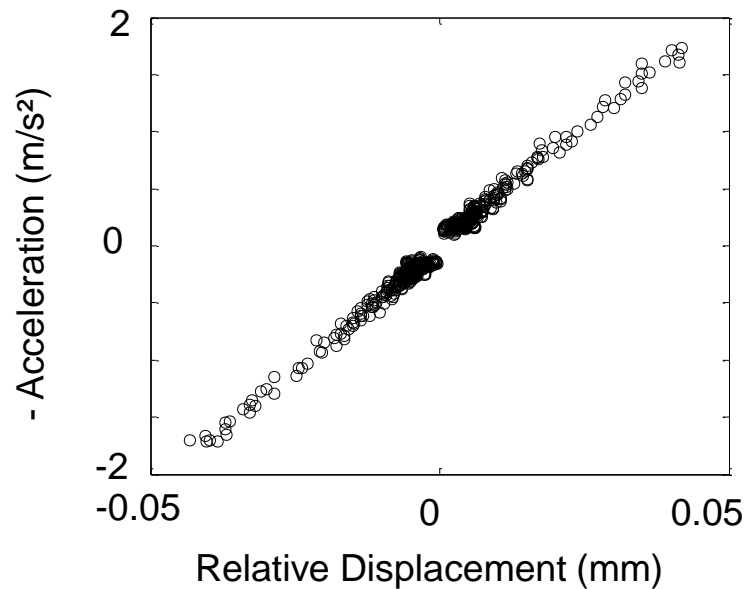
Linear Behavior at Low Level



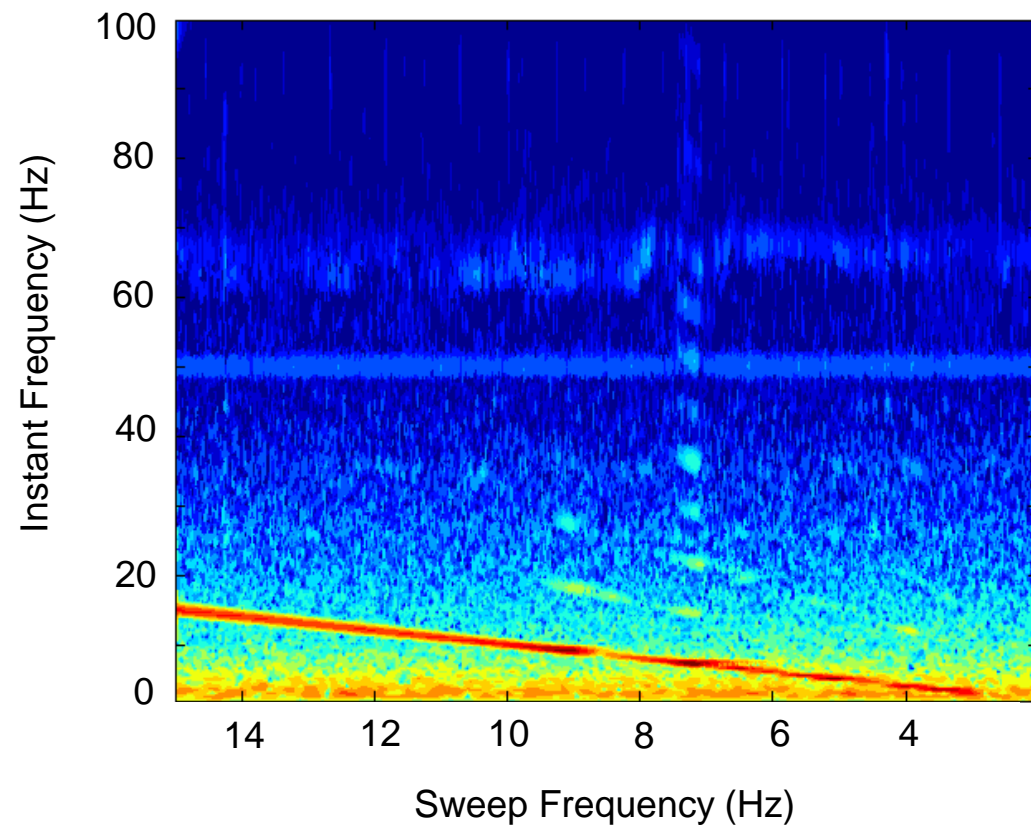
Sine sweep down of 4.8N



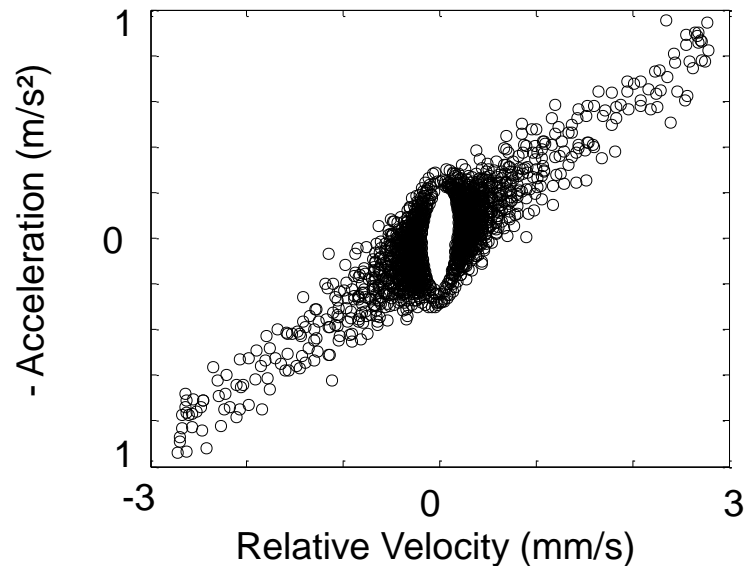
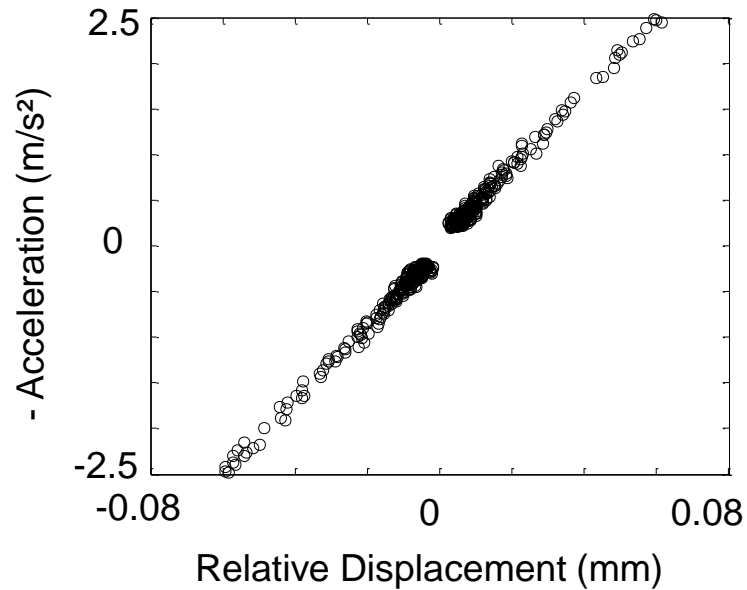
Hysteresis Visible in the Damping Curve



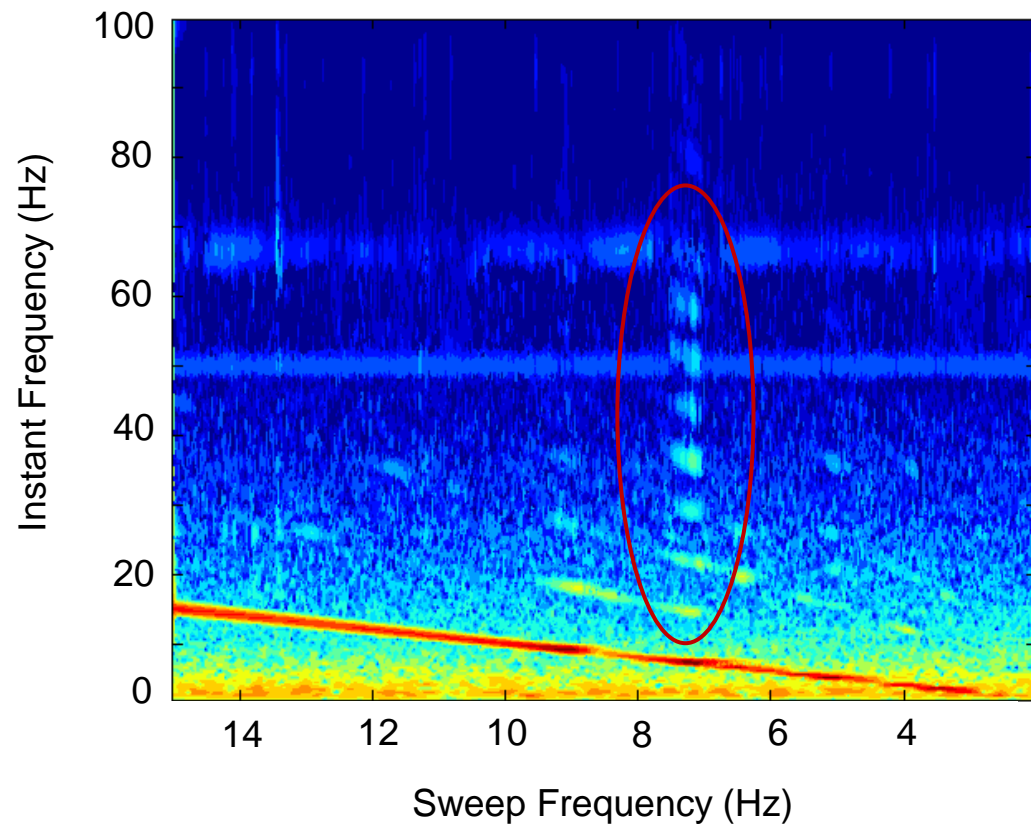
Sine sweep down of 9.6N



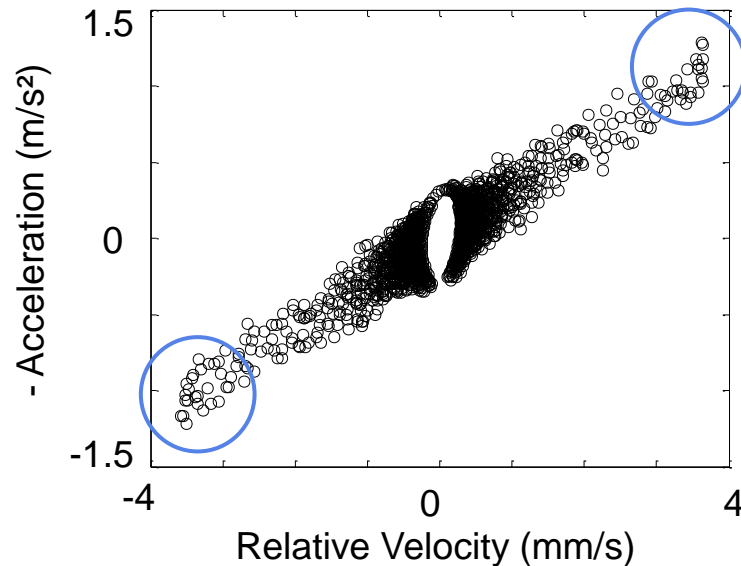
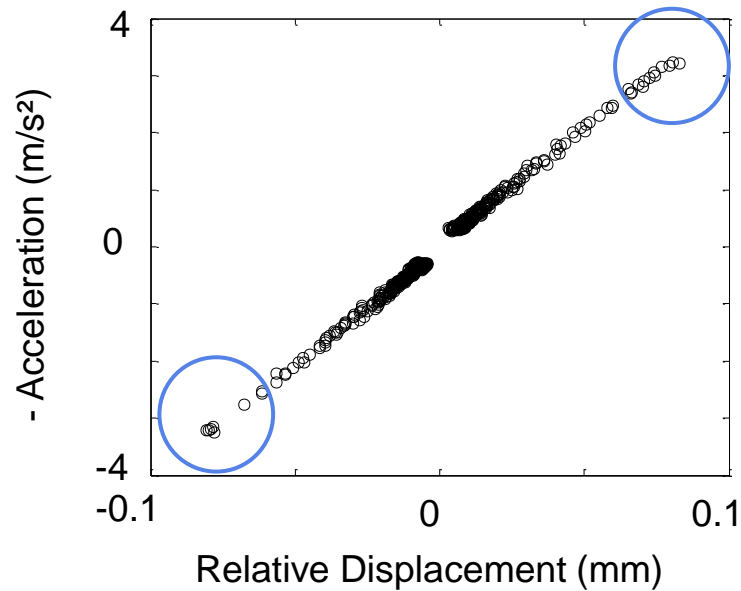
Harmonics Appear Around the Third Mode



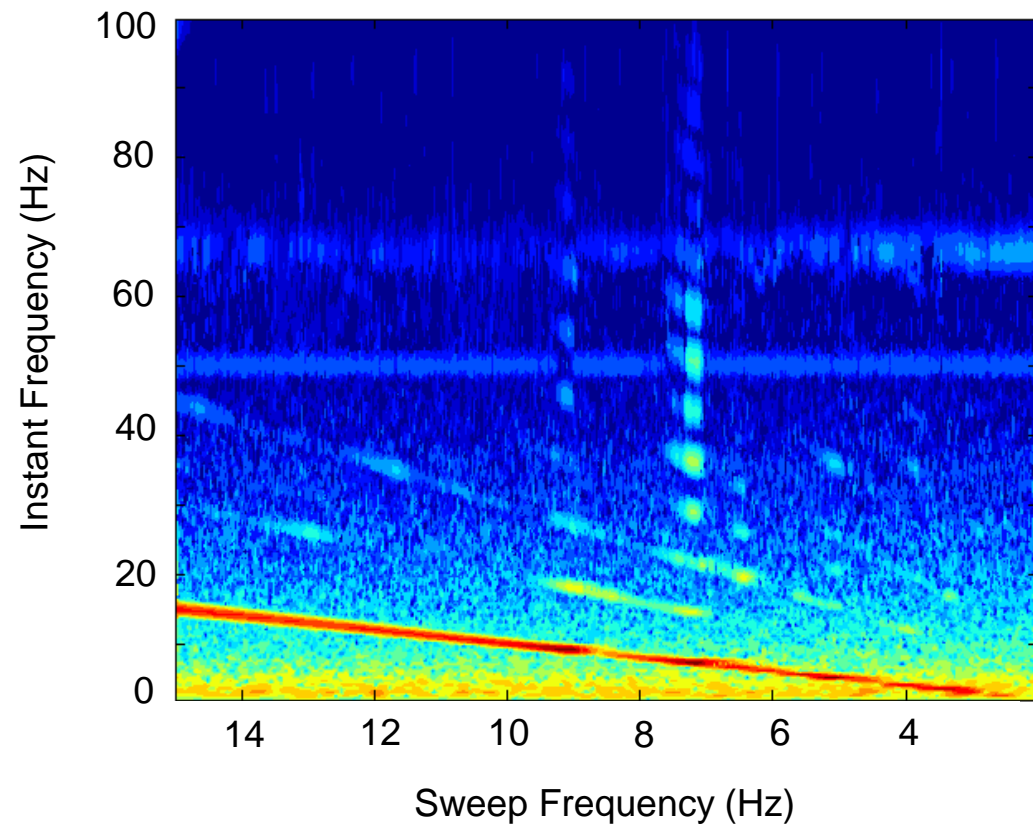
Sine sweep down of 14.4N



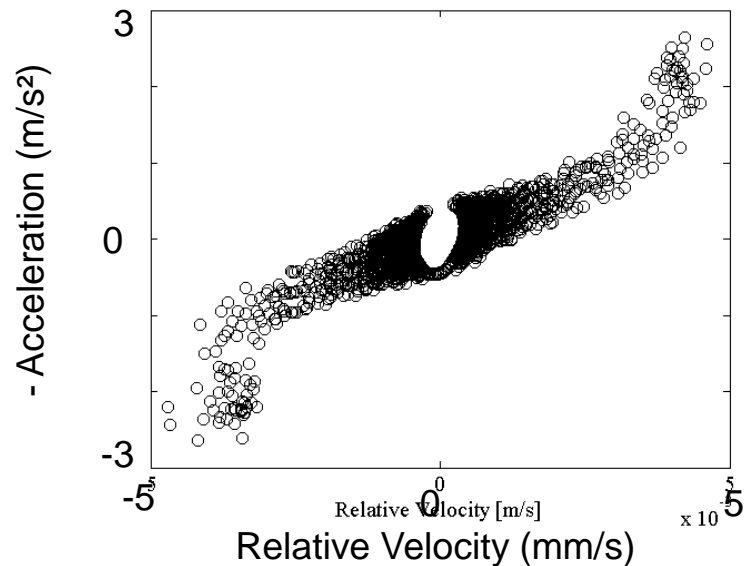
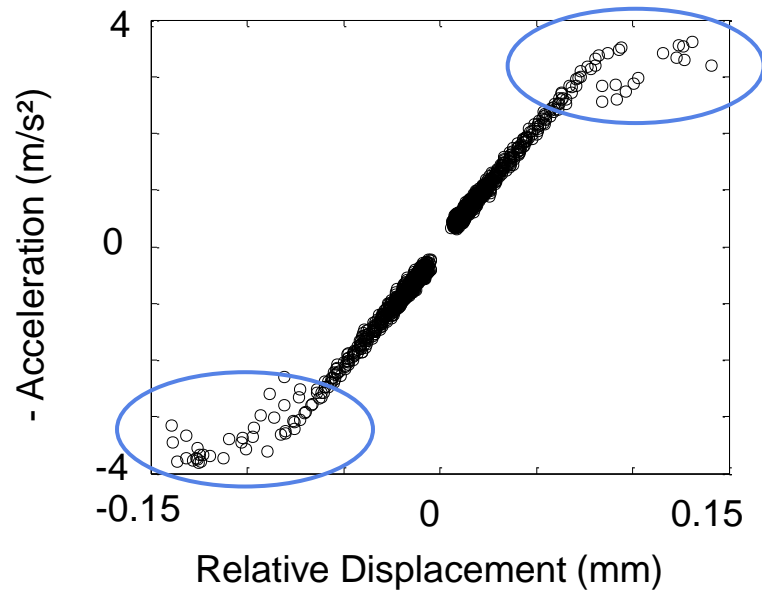
Extremities of Curves Indicate New Regime



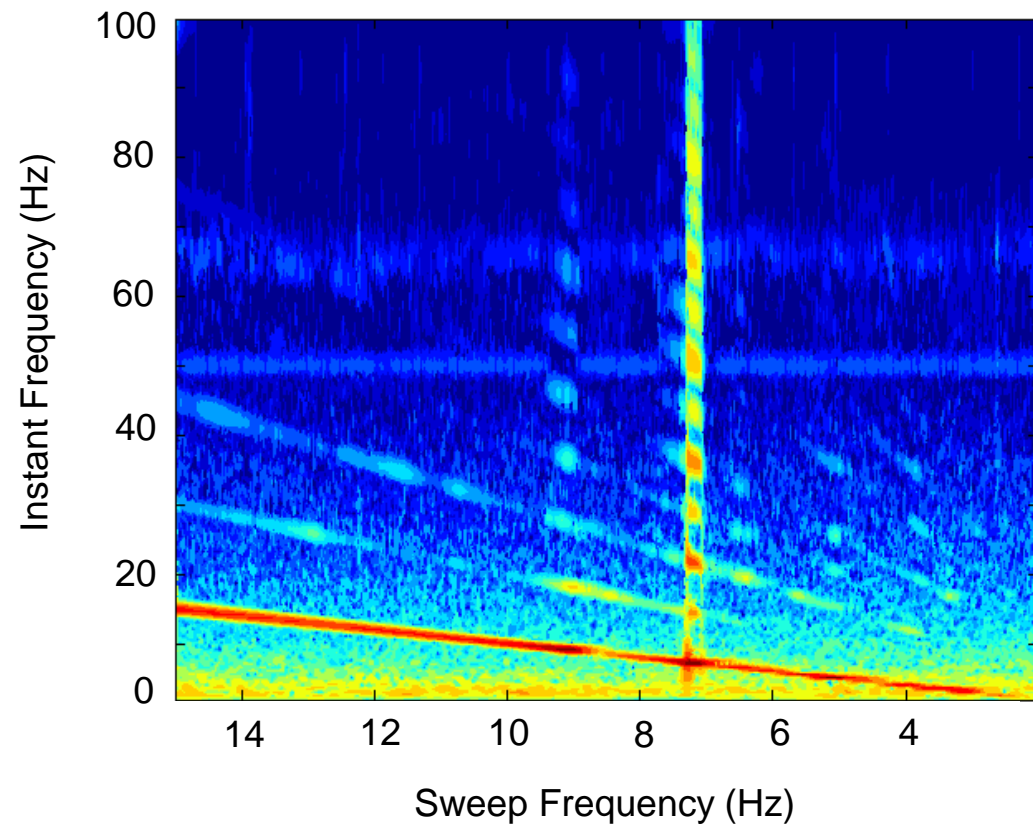
Sine sweep down of 19.2N



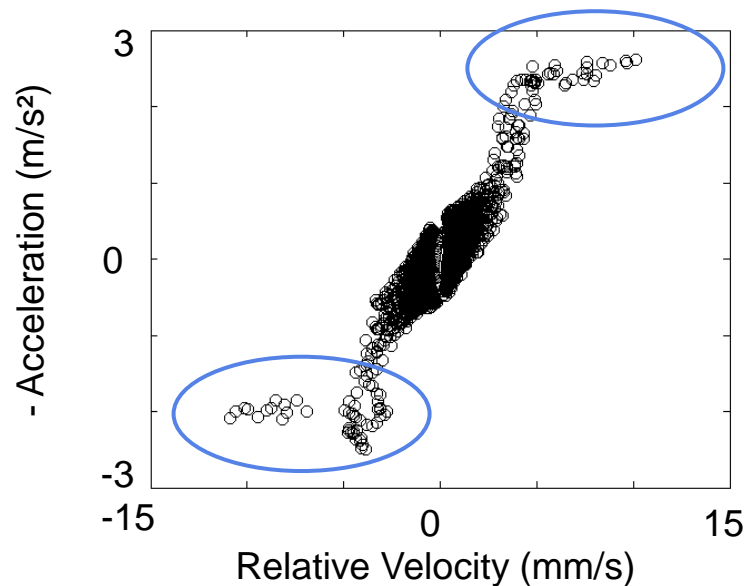
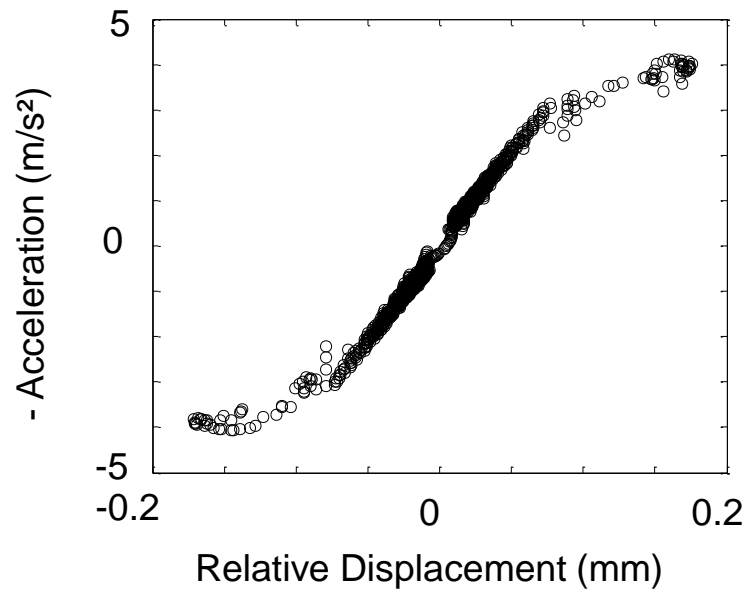
Joint Opening Causes Softening



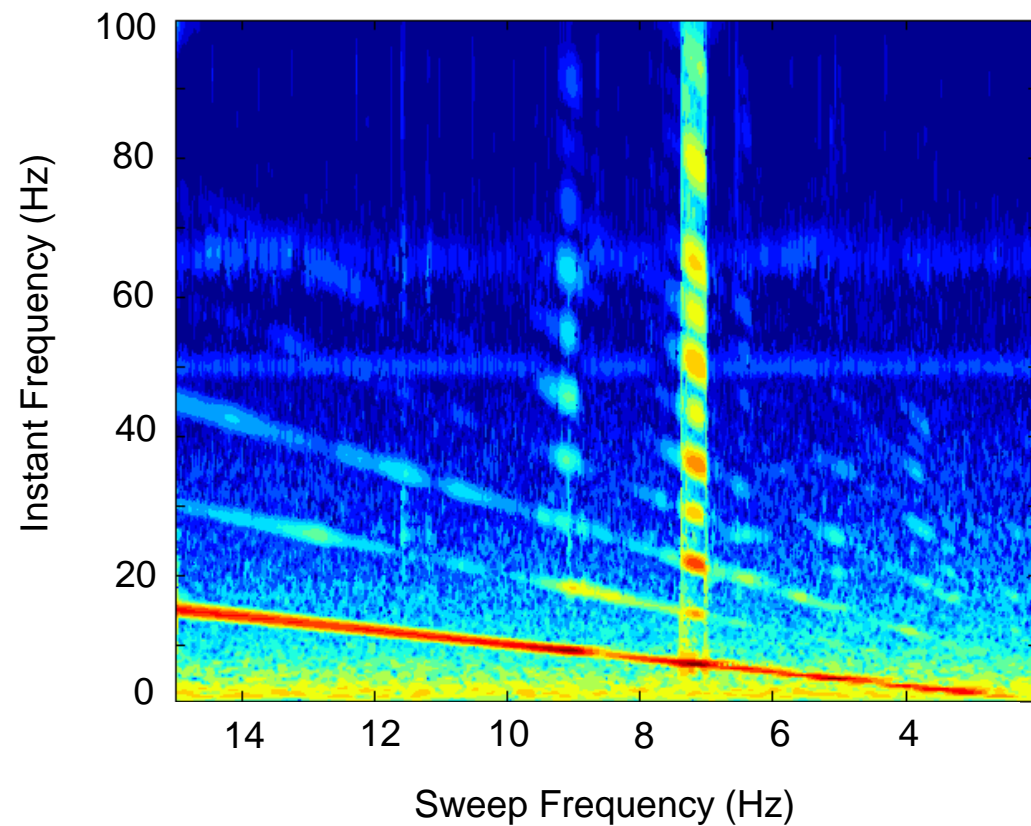
Sine sweep down of 28.8N



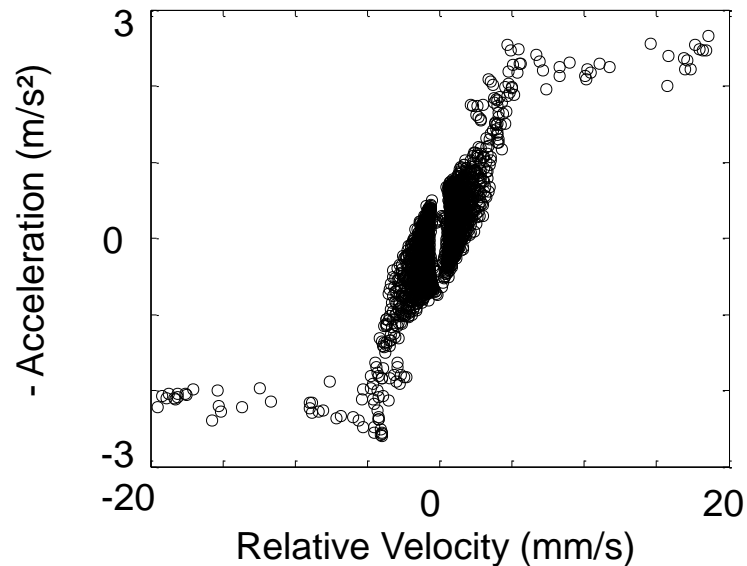
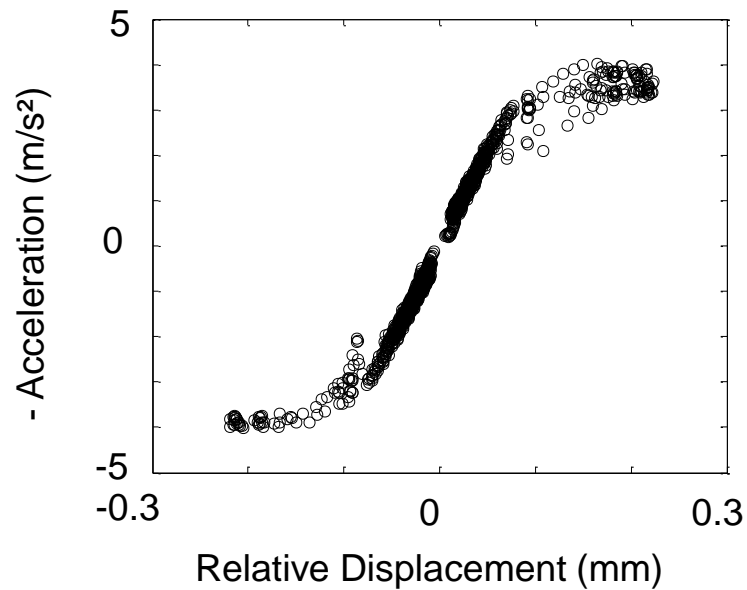
Coulomb Friction Identified



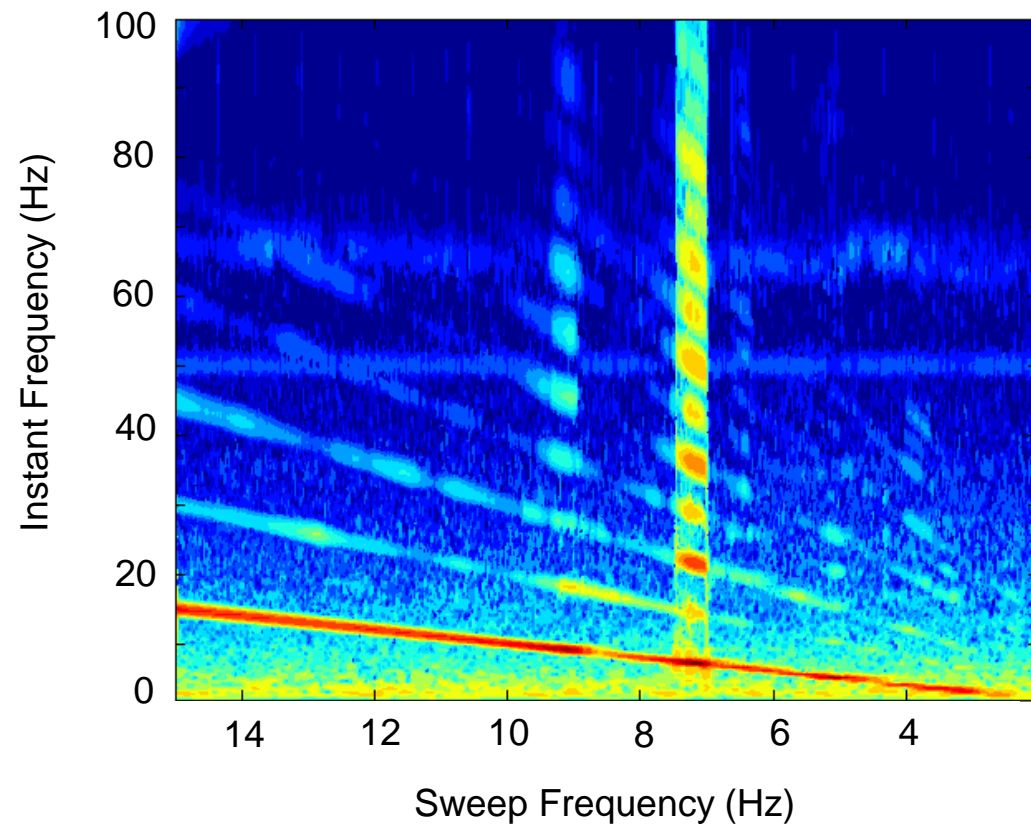
Sine sweep down of 38.4N



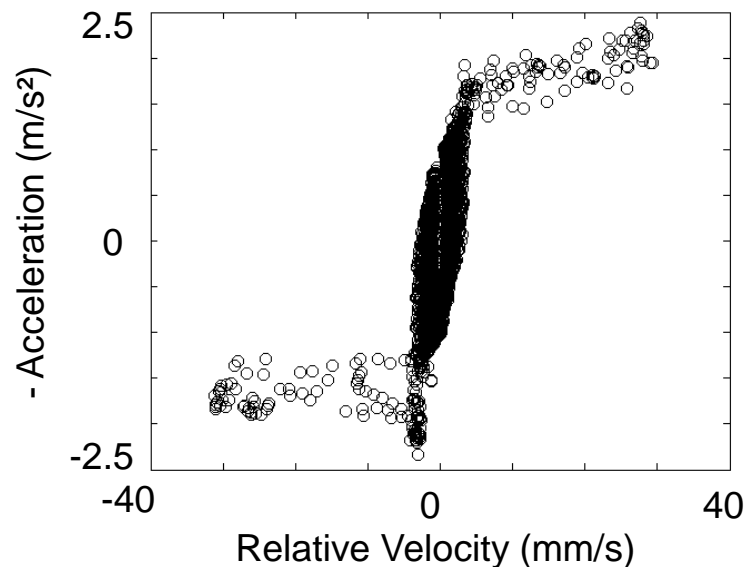
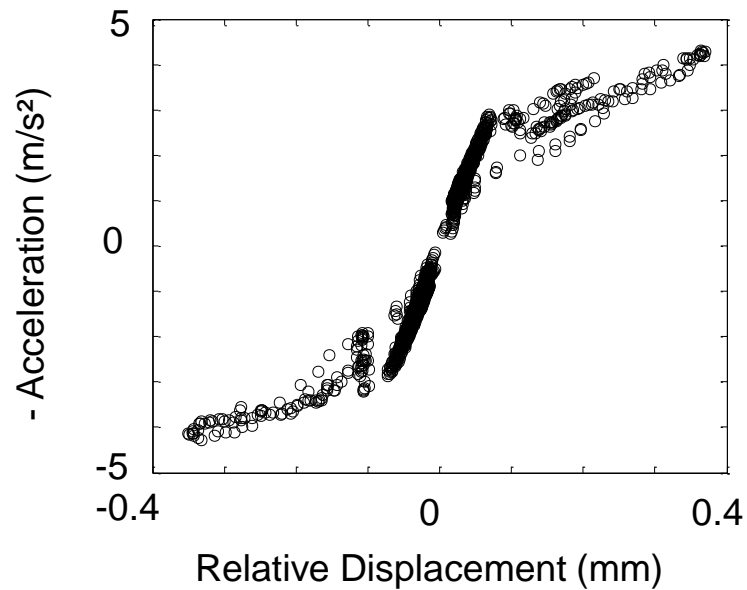
Softening and Coulomb Friction Remain at Higher Levels



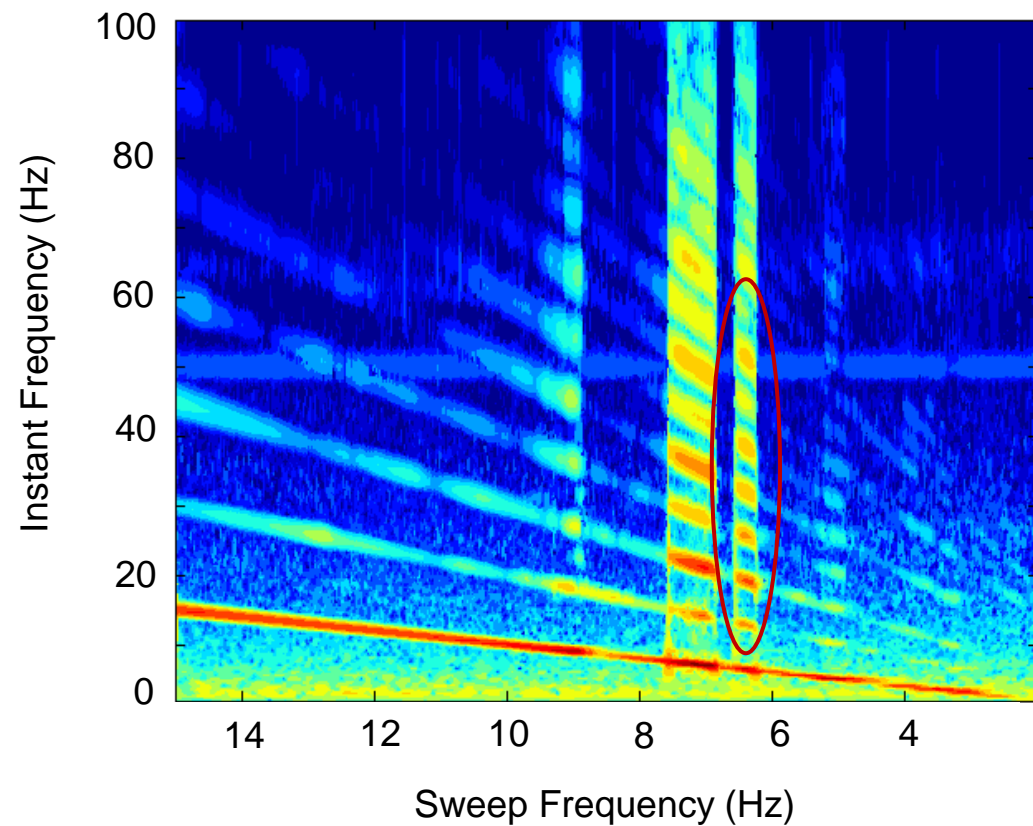
Sine sweep down of 48N



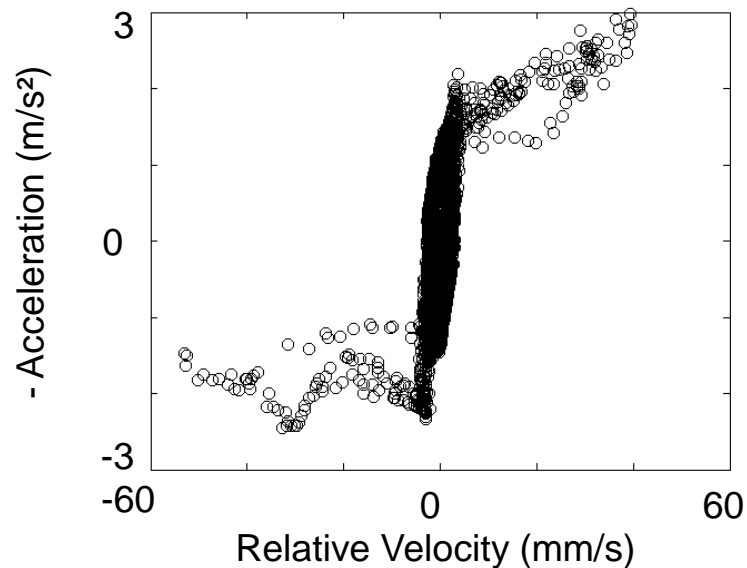
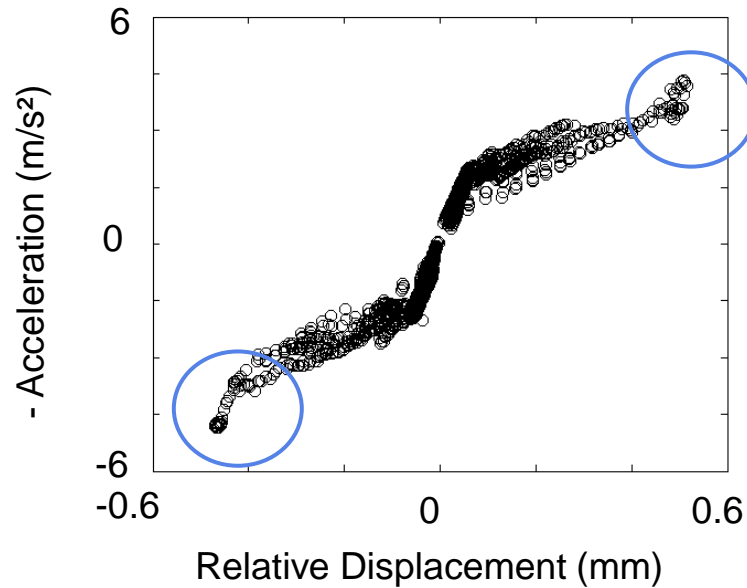
The Second Mode Becomes Highly Nonlinear Too



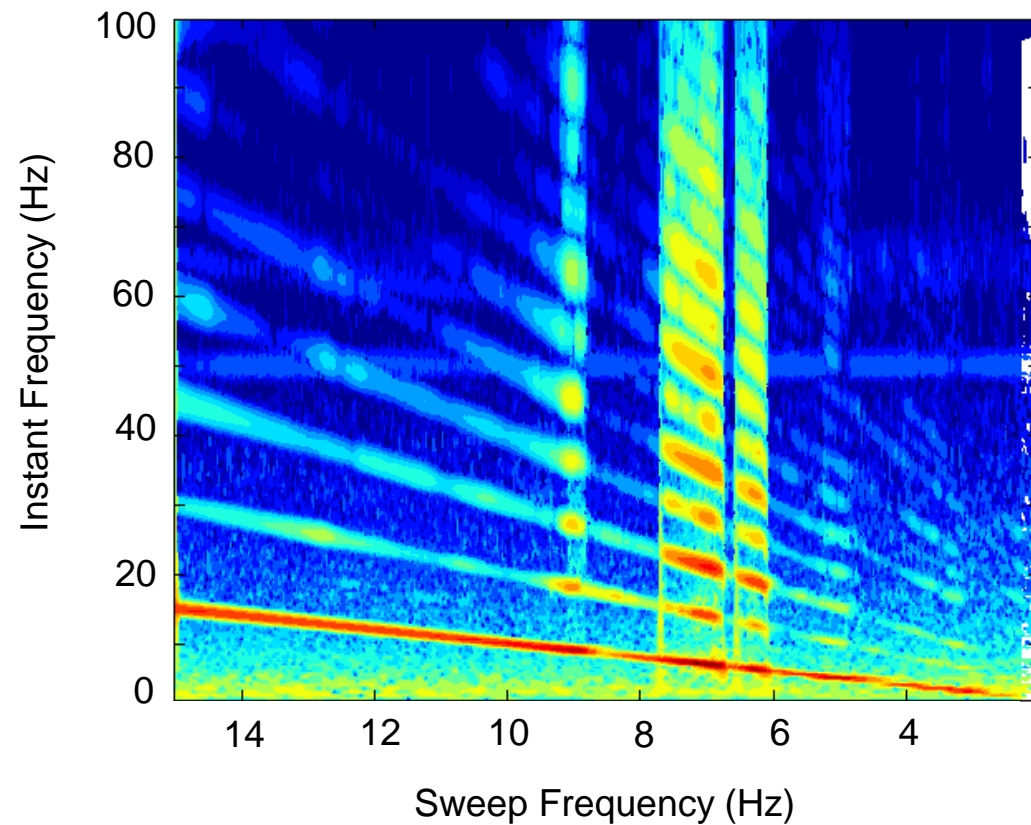
Sine sweep down of 67N



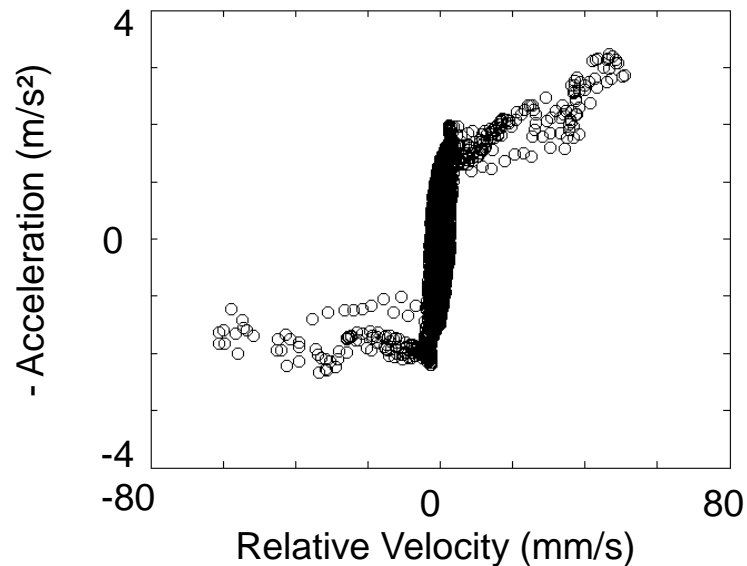
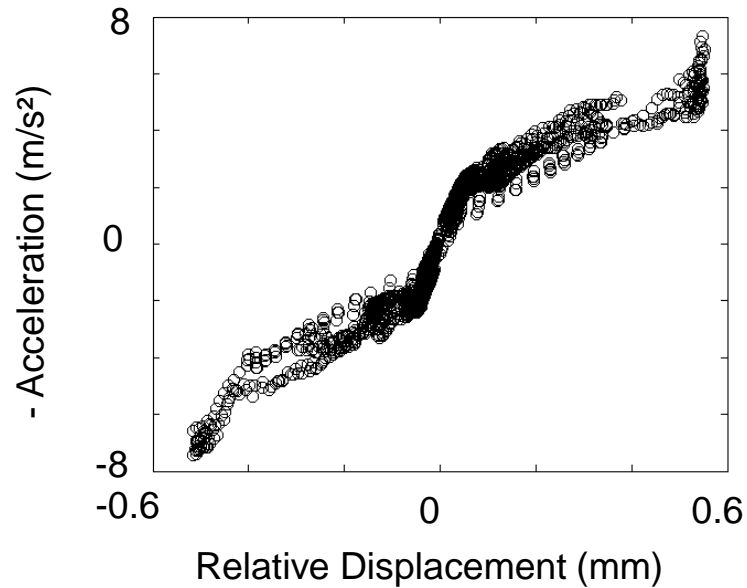
Impacts Occur for High Relative Displacements



Sine sweep down of 86N

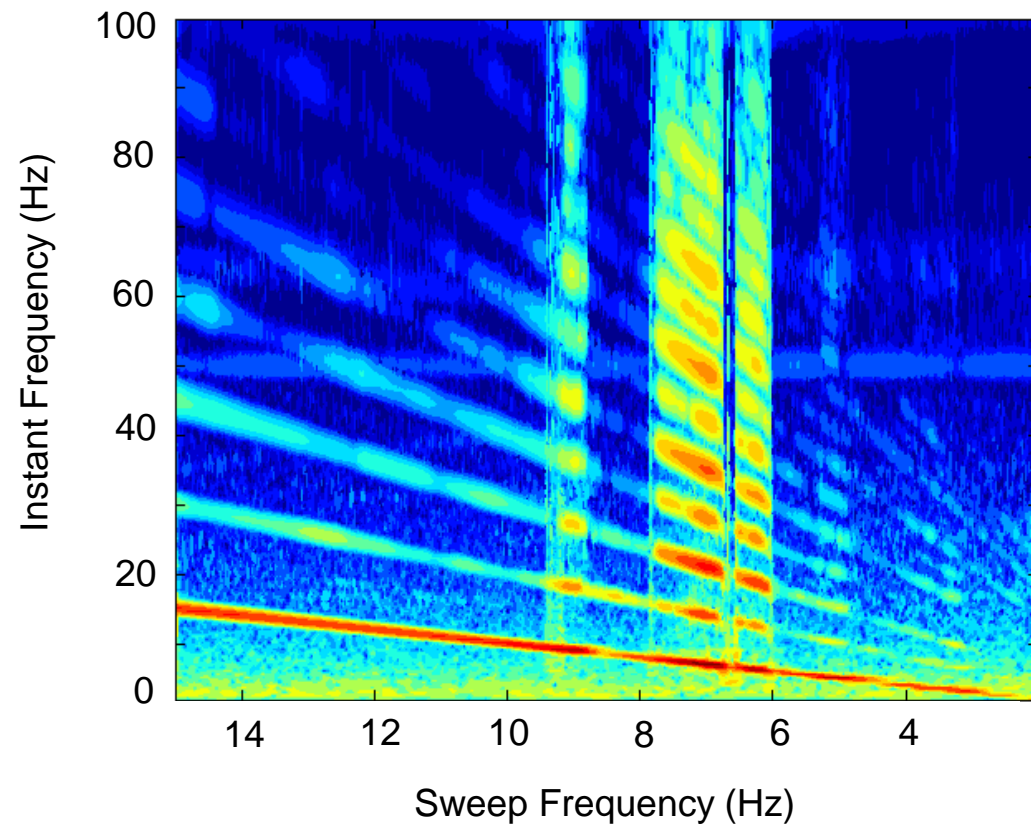


High Level Fully Reveals the Nonlinear Mechanisms

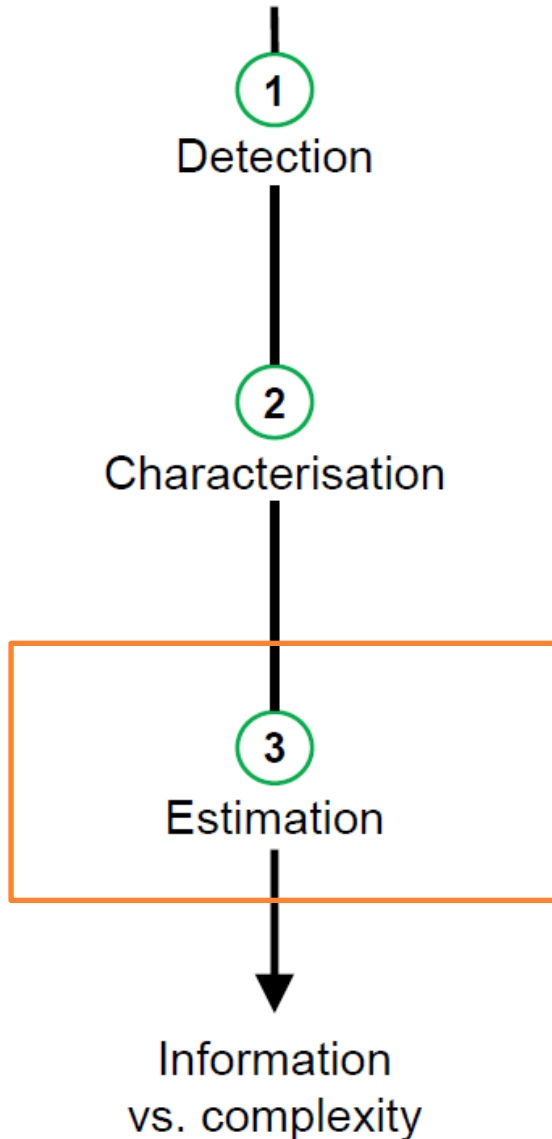


Sine sweep down of 95.6N

Wide harmonics



The Nonlinear System Identification Process



Do I observe nonlinear effects? **YES**

Should I build a nonlinear model? **YES**

Where is the nonlinearity located ? **WING TIP**

What is the underlying physics? **IMPACTS**

What mathematical model? **PIECEWISE LIN.**



Model parameters?

How uncertain are they?

Finite Element Model of the F-16 Wing

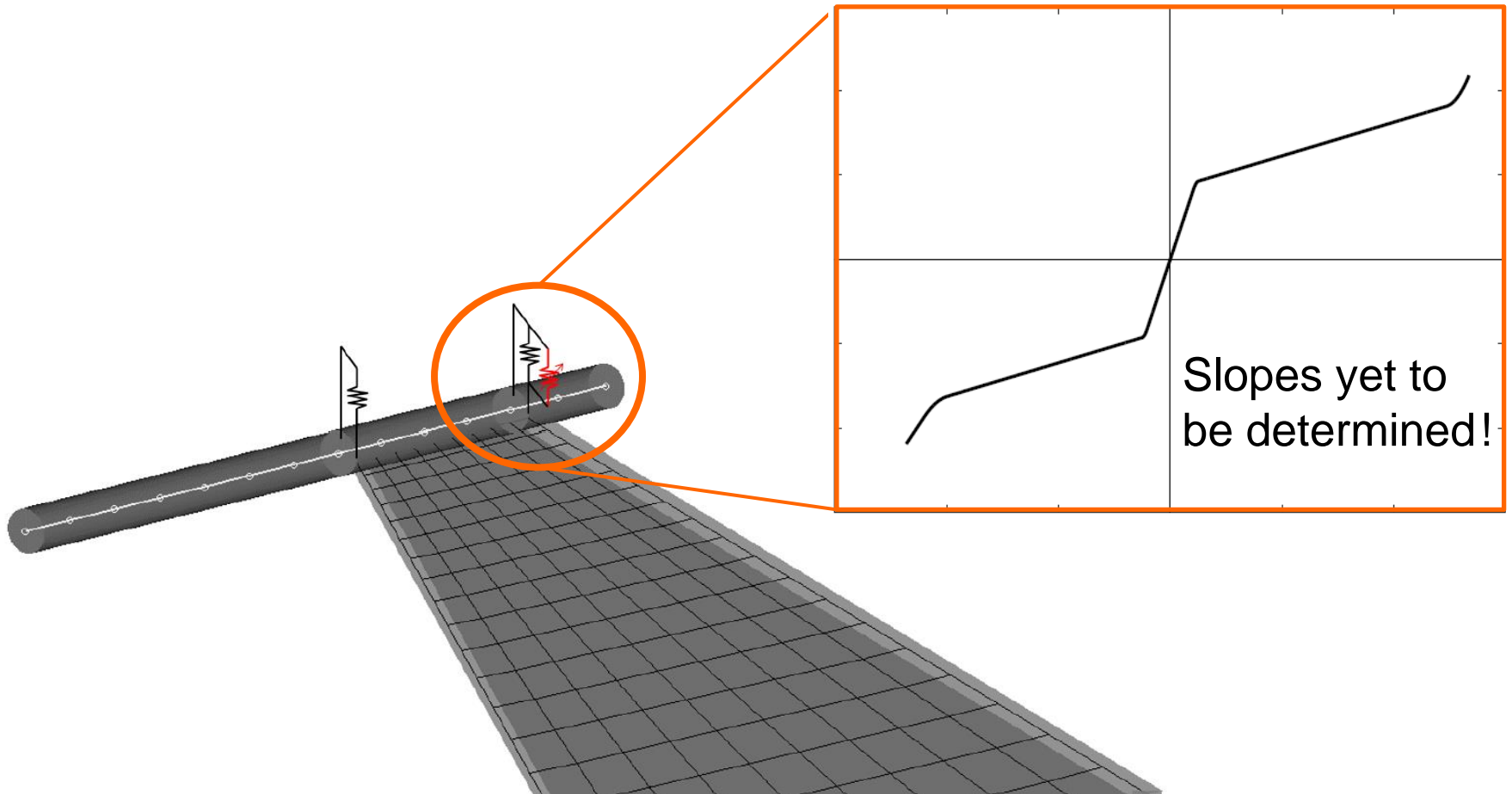


Table 2 Nonlinear parameters of the piecewise-linear spring and damper

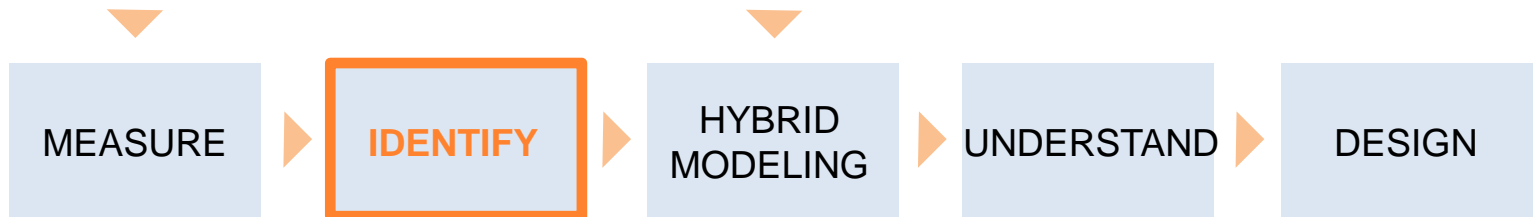
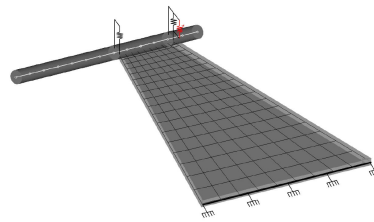
Nonlinear element	Clearances	Slopes
Spring	$[-4.09 ; -0.04 ; 0.05 ; 5.40] \times 10^{-4} \text{m}$	$[0.60 ; 0.16 ; 0.60 ; 0.14 ; 1.72] \times 10^7 \text{N/m}$
Damper	$[-0.54 ; -0.41] \times 10^{-2} \text{m/s}$	$[-0.05 ; 5.51 ; 0.65] \times 10^4 \text{Ns/m}$

Concluding Remarks

VIBRATION
MEASUREMENTS



LINEAR FINITE
ELEMENT MODEL



Detection
Characterization
Parameter estimation

Nonlinear modes
Nonlinear FRFs
Bifurcations

Input and Output Measurements for Nonlinear ID

Checklist:

1. Did you select appropriate excitation signals?
2. Did you record response signals properly?
3. Did you measure enough data?

Specifically,

Increase the sampling frequency.

Record time histories, not spectra.

Record throughput time histories, do not average/filter upfront.

Store the input signal. Consider multiple levels of excitation.

Instrument potential nonlinearities with sensors on both sides.

Thank you for your attention.

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University of Liège, Belgium

